

**Raman spectroscopy and x-ray diffraction of phase transitions in Cr<sub>2</sub>O<sub>3</sub> to 61 GPa**

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Raman spectroscopy and x-ray diffraction measurements have been performed for pure Cr<sub>2</sub>O<sub>3</sub> to 61 GPa at ambient temperature with and without laser heating. Several changes were found at 15–30 GPa under cold compression: splittings of two  $E_g$  phonons, steep selective increase of some phonon intensities, softening of low-frequency phonon modes, selective broadening of some diffraction lines, systematic deviation of diffraction positions relative to the corundum structure assignment, and eventual splitting of the (110)<sub>H</sub> diffraction line at 58 GPa. These changes are consistent with those expected for a phase transition to the monoclinic V<sub>2</sub>O<sub>3</sub>-type ( $I2/a$ ) structure. Another phase transition has been found above 30 GPa after laser heating. This is accompanied by considerable changes in Raman spectra and diffraction patterns, which implies that the transition is reconstructive. The diffraction patterns of this phase can be well explained by either of the orthorhombic structures, perovskite or Rh<sub>2</sub>O<sub>3</sub>-II type. This confirms the recent prediction of stability of an orthorhombic phase in Cr<sub>2</sub>O<sub>3</sub> at high pressure by first-principles calculations. Color changes of Cr<sub>2</sub>O<sub>3</sub> were also detected: from green to red at 14 GPa during cold compression and from red to green during the phase transition to the orthorhombic phase above 30 GPa. Detailed analyses on diffraction patterns show that the color changes are relevant to Cr-O bond-length change. Furthermore, the observed variation trends of bond lengths in Cr<sub>2</sub>O<sub>3</sub> during cold compression are similar to those in Al<sub>2</sub>O<sub>3</sub> with much more pressure sensitivity, which is consistent with recent first-principles calculations, but are opposite to those in V<sub>2</sub>O<sub>3</sub> and Fe<sub>2</sub>O<sub>3</sub> at high pressure.

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**I. INTRODUCTION**

3d-transition metal sesquioxides have attracted a great deal of attention with regard to their electromagnetic properties and structural changes.<sup>1</sup> Whereas many of these sesquioxides ( $M_2O_3$ ,  $M = \text{Ti, V, Cr, Fe}$ ) have the corundum structure ( $R\bar{3}c$ ,  $D_{3d}^6$ ) at ambient conditions, various types of transitions have been reported for different sesquioxides at high pressure and high temperature with different changes in crystal structure, or electromagnetic properties: No crystallographic changes occur for the insulator-to-semiconductor transition in Ti<sub>2</sub>O<sub>3</sub> at 390–470 K and ambient pressure.<sup>2,3</sup> In (V<sub>1-x</sub>Cr<sub>x</sub>)<sub>2</sub>O<sub>3</sub> ( $x = 0.0-0.12$ ), a structural transition to a monoclinic phase ( $I2/a$ ,  $C_{2h}^6$ ) is accompanied with a transition from a paramagnetic semiconductor to an antiferromagnetic insulator at low temperature or high pressure depending on composition.<sup>4,5</sup> Fe<sub>2</sub>O<sub>3</sub> transforms to a metallic orthorhombic phase (Rh<sub>2</sub>O<sub>3</sub>-II or perovskite type) at 55 GPa (Refs. 6 and 7). Thus, investigation of Cr<sub>2</sub>O<sub>3</sub> at high pressure is of interest to further explore structural changes in the transition metal oxides.

A phase transition in Al<sub>2</sub>O<sub>3</sub> from the corundum to the

Rh<sub>2</sub>O<sub>3</sub>-II structures at 78 GPa was proposed on the basis of first-principles calculations.<sup>8</sup> A later x-ray diffraction study<sup>9</sup> reported changes at 100 GPa which could be interpreted as evidence for this transition. However, the resolution of the diffraction patterns was not sufficient to be conclusive. In the proposed mechanism for the phase transition in ruby (Cr-doped Al<sub>2</sub>O<sub>3</sub>), CrO<sub>6</sub> octahedra in the ruby structure are thought to be the critical units that trigger the phase transition.<sup>10</sup> Since ruby is widely used as a pressure calibrant in high-pressure studies, understanding the nature of ruby phase transitions is of broad interest. Another first-principles calculation<sup>11</sup> also predicts that pure Cr<sub>2</sub>O<sub>3</sub> may transform to the Rh<sub>2</sub>O<sub>3</sub>-II structure at much lower pressure, 15 GPa. While Raman spectra<sup>12</sup> have shown clear evidence for an unknown structural transition above 13 GPa, x-ray-diffraction studies<sup>12,13</sup> have not found any evidence for the structural change to 30 GPa. This discrepancy has not been resolved.

Here we present the results of measurements using Raman spectroscopy and x-ray diffraction and visual observations for pure Cr<sub>2</sub>O<sub>3</sub> to 61 GPa at 300 K with and without laser

heating. Several lines of evidence for a phase transition at 15–30 GPa were found when  $\text{Cr}_2\text{O}_3$  is compressed at 300 K. We also report the Raman spectra and diffraction patterns of the orthorhombic phase observed after laser heating above 30 GPa. We will discuss the crystal structures of the high-pressure phases and structural response of  $\text{Cr}_2\text{O}_3$  to stress.

## II. EXPERIMENTAL TECHNIQUES

Pure synthetic  $\text{Cr}_2\text{O}_3$  (Aldrich, 99.995%) was used as starting material. The purity and crystal structure (corundum type) were confirmed using x-ray diffraction and Raman spectroscopy at ambient conditions. Powdered  $\text{Cr}_2\text{O}_3$  was loaded in the 100  $\mu\text{m}$  hole of an indented stainless steel gasket and compressed between two 300  $\mu\text{m}$  culet low-fluorescence diamond anvils. A symmetric-type diamond cell with 60° conical apertures and a Mao-Bell-type diamond cell with slot shaped apertures were used. Small ruby chips were loaded for pressure measurements using the quasihydrostatic ruby pressure scale.<sup>14</sup> Argon was cryogenically loaded into the sample chamber as a pressure transmitting and thermal-insulating medium. For Raman measurements below 10 GPa, we used a methanol-ethanol (4:1) mixture as a pressure medium.

Raman spectra were excited using an argon-ion laser ( $\lambda = 514.5$  nm) and recorded with a single spectrometer at Princeton University<sup>7</sup> and with a triple spectrometer at Livermore National Laboratory. A spectral range of 150–1250  $\text{cm}^{-1}$  was used for measurements to 62 GPa. The spectrometers were frequently calibrated using Ne emission spectra over the course of the experiments. In order to prevent sample heating by the argon-ion laser, we loaded the sample directly in contact with a high thermal-conductivity diamond anvil and measured spectra from this contact surface. For laser heating experiments, we separated the sample foils from the diamond anvils by loading argon below and above the samples to reduce heat loss through the anvils. Raman spectra were typically collected over 10 min. Peaks were fitted using a Lorentzian profile shape function. For asymmetric peaks we used a split Pearson VII function.

Angle-dispersive x-ray diffraction measurements were performed at the B2 sector of the Cornell High Energy Synchrotron Source (CHESS) and at the 10.3 sector of the Stanford Synchrotron Radiation Laboratory (SSRL) using monochromatic x-ray beams ( $\lambda = 0.4959$  Å at CHESS and 0.7277 Å at SSRL) and imaging plates. Two diffraction patterns were measured at each pressure at different distances from the sample. The sample-imaging plate distances were measured using the diffraction lines of NaCl and MgO. The backing plates of the symmetric cell restricted the maximum value of  $2\theta$  to  $\sim 16^\circ$ . In order to obtain a wider angle range, we tilted the symmetric type diamond cell with respect to the incident x-ray beam. This allows us to measure spectra to  $\sim 28^\circ 2\theta$ . However, instead of full diffraction rings, we obtained partial rings (160° arc) due to the tilting. With the Mao-Bell-type cell, since it has a slot aperture, we were able to measure diffraction patterns to  $\sim 40^\circ 2\theta$  without tilting. However, the slot-type aperture only allows 8°–10° arc of diffraction rings. In these experiments, pressure was mea-

sured using the argon equation of state<sup>15</sup> in addition to the ruby scale. Some of samples were heated using a cw Nd:YAG laser (where YAG stands for yttrium aluminum garnet). The entire sample was scanned by the laser for 15–20 min to anneal differential stresses or synthesize a high-temperature phase.

Geometric corrections for the measured diffraction images were performed using the program SIMPA.<sup>16</sup> Integrations to obtain one-dimensional patterns were carried out for the portion of the rings ( $\sim 60^\circ$ ) where the maximum  $2\theta$  angle range is achieved for the patterns measured with the symmetric-type cell. Individual peak fitting using a pseudo-Voigt profile function was performed to obtain the unit-cell parameters. Unit-cell refinements were performed using the UNITCELL code.<sup>17</sup> GSAS (Ref. 18) was used for Rietveld refinement and Le Bail fitting.

We also performed energy-dispersive x-ray diffraction measurements at *in situ* high  $P$ - $T$  (25–30 GPa and 1500–2000 K) at the GSECARS sector of the Advanced Photon Source. A double-sided laser heating system<sup>19</sup> with a cw Nd:YLF laser was used in this experiment.

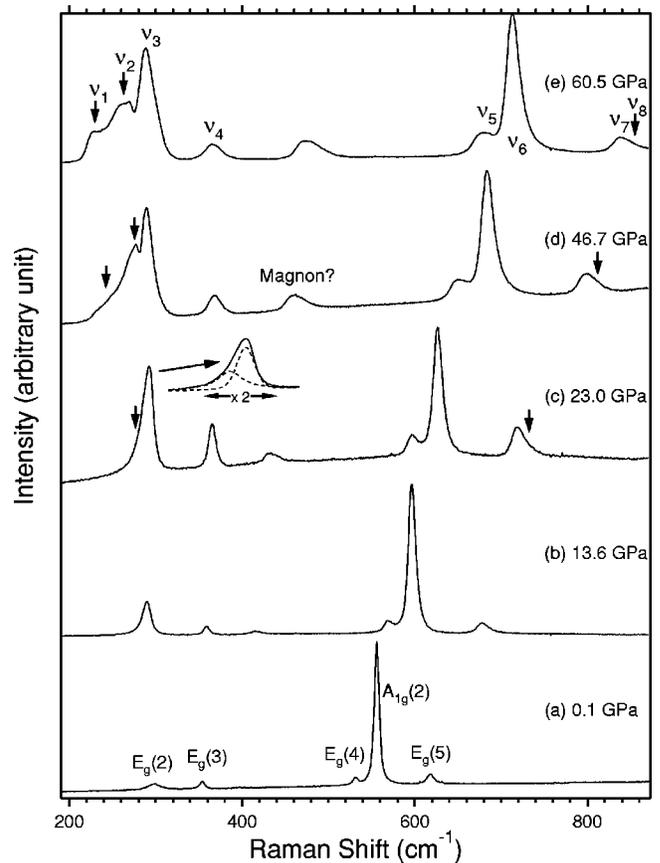


FIG. 1. High-pressure Raman spectra of  $\text{Cr}_2\text{O}_3$  measured at 300 K without laser heating. Peak assignments for the corundum-type phase follow from single-crystal measurements (Ref. 21). New features observed above 15–30 GPa during cold compression are indicated by arrows ( $\nu_1$ ,  $\nu_2$ , and  $\nu_8$ ). An example for the peak fit for  $E_g(2)$  using two peaks ( $\nu_2$  and  $\nu_3$ ) is shown (dashed lines) together with the observed spectrum (solid line) in the inset. Pressure is shown above each trace.

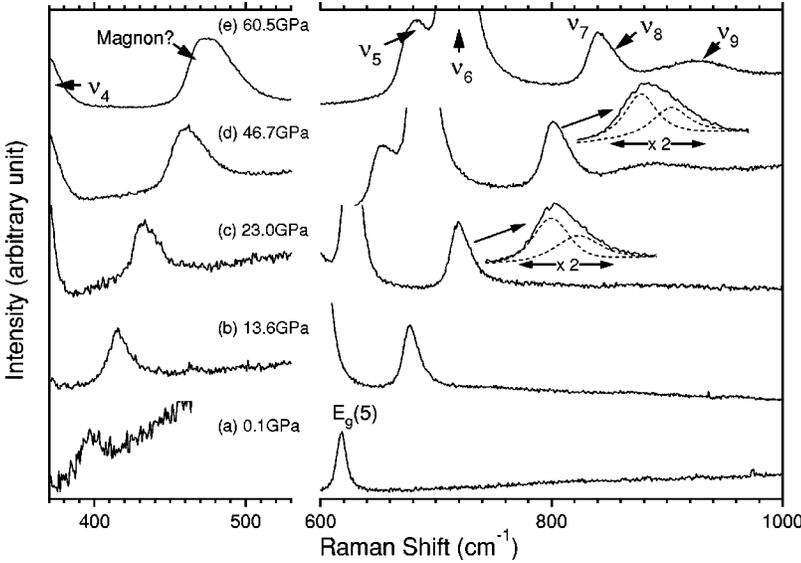


FIG. 2. Raman spectra of the mode at 400–450  $\text{cm}^{-1}$ , which has been assigned as a magnon in previous studies (Ref. 21), and selected phonon modes at 600–1000  $\text{cm}^{-1}$  at high pressures and ambient temperature. Examples for the peak fit for  $E_g(5)$  using two peaks ( $\nu_7$  and  $\nu_8$ ) are shown (dashed lines) together with the observed spectra (solid lines) in the insets. Notation is the same as in Fig. 1.

III. RESULTS

A. Phase transition at 15–30 GPa and 300 K

Raman spectra were measured to 60.5 GPa at 300 K without heating (Figs. 1–3). We compare the measured Raman shifts at the lowest pressure (0.09 GPa) with previous ambient pressure studies in Table I. The different studies are generally in agreement within a few wave numbers. Two different single-crystal polarization measurements<sup>20,21</sup> agree on the mode assignment except for a mode in the 290–304  $\text{cm}^{-1}$  range. We use the assignment<sup>21</sup> which is consistent with that for  $V_{1-x}Cr_xO_3$  (Ref. 22). Two weak modes below 270  $\text{cm}^{-1}$

were not observed in our powder Raman spectra as was also the case for other powder Raman studies.<sup>12,23</sup>

With compression, we observed a relative intensity increase [Figs. 1(a), 1(b), and 4] and frequency decrease (Fig. 3) of  $E_g(2)$  mode to 15 GPa. Above 15 GPa, two phonon modes  $E_g(2)$  and  $E_g(5)$  become asymmetric [see the insets of Figs. 1(c) and 2(c), and Fig. 3]. Upon further compression, clear splitting of  $E_g(2)$  into a doublet ( $\nu_2$  and  $\nu_3$ ) was observed, and a broad band ( $\nu_1$ ) also appears at  $\sim 250 \text{ cm}^{-1}$  above 26 GPa [Figs. 1(d), 1(e), and 3]. Mougín *et al.*<sup>12</sup> observed this splitting as well, but incorrectly attributed it to pressure gradients in the sample. While we were not able to

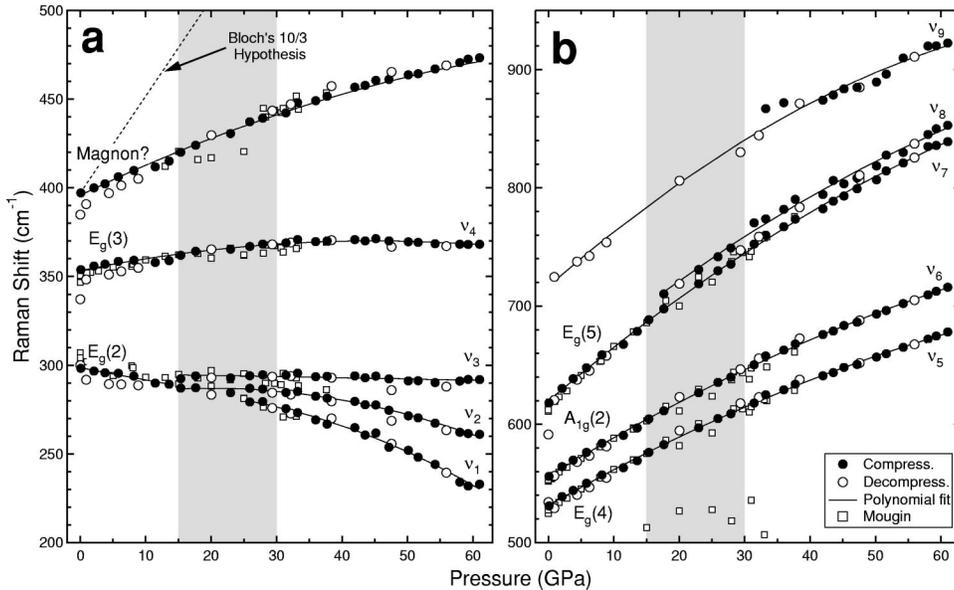


FIG. 3. Pressure shift of Raman modes at high pressure and 300 K without laser heating. Solid circles are the data points for compression and open circles are for decompression. Polynomial fits for compression data are shown as solid lines. The polynomial fit for  $\nu_9$  also includes decompression data points. Lower pressure Raman measurements (Ref. 12) are plotted for comparison (open squares). Assignments follow from single-crystal polarization measurements (Ref. 21). The predicted magnon frequency change with compression by Bloch's hypothesis (Ref. 25) is plotted as a dashed line in (a). The shaded area indicates where changes in Raman spectra were detected during cold compression and decompression. Peak assignments are the same as in Fig. 1.



the observed intensity jumps in this pressure range. In addition, this peak becomes asymmetric above 20 GPa (Fig. 2).

Bloch<sup>25</sup> has proposed that the mode Grüneisen parameter  $\gamma$  for magnons may be close to  $10/3$ . We calculated the expected variation of the Raman frequency  $\nu$  if this hypothesis is valid for  $\text{Cr}_2\text{O}_3$ , using the following equation:

$$\gamma = -\frac{d \ln \nu}{d \ln V} = \frac{K_T}{\nu} \left( \frac{d\nu}{dP} \right). \quad (1)$$

The bulk modulus  $K_T$  ranges from 230 to 240 GPa (Refs. 26 and 27). The lower bound result for the pressure behavior of this mode is shown in Fig. 3(a), provided that the mode is due to magnon-photon interaction and follows Bloch's hypothesis. The observed pressure variation of the mode is very different from what is expected from Bloch's hypothesis, and its Grüneisen parameter is calculated to be  $1.06 \pm 0.03$  from our data.

Bloch's hypothesis is based on a variety of empirical trends. However, the accessible pressure range was limited at that time. Recently it has been shown that the magnon  $\gamma$  ranges from 1.6 to 3.3 and may be material dependent in contrast to Bloch's hypothesis: 1.7–2 for  $\text{La}_2\text{CuO}_4$  (Ref. 28),  $2.7 \pm 0.2$  for  $\text{CoO}$  (Ref. 29), and 2.3–2.6 for  $\text{NiO}$  (Ref. 30). In fact, Bloch's hypothesis considers only up to second neighbor interactions, whereas it has been shown that the relatively complicated corundum-type lattice requires to take into account up to fourth neighbor interactions.<sup>31</sup> It is notable that  $\gamma = 1.06$  is the lowest ever reported for magnons and a significant nonlinearity of the pressure-induced shift is observed.

However, we cannot rule out a phonon assignment for this mode. Its mode  $\gamma$  is very close to other phonon mode  $\gamma$ 's. One possibility is that a new phonon mode appears due to the phase transition and its frequency coincides with the magnon. However, it should be noted that  $\gamma$  is already very low even below the phase transition pressure [Fig. 3(a)].

We also observed a broad band near  $700 \text{ cm}^{-1}$  above 30 GPa during compression which is preserved upon decompression [ $\nu_9$  in Figs. 2 and 3(b)]. A similar feature was observed near this range in  $(\text{Fe}_{1-x}\text{Cr}_x)_2\text{O}_3$  ( $x = 0.0-0.8$ , Refs 23 and 7) and assigned as an IR-active and Raman-inactive mode that appeared in Raman spectra due to surface- or pressure-induced defects. An IR measurement at ambient pressure<sup>32</sup> reported features near this range [ $E_u(\text{TO}) = 734 \text{ cm}^{-1}$  and  $A_{2u}(\text{TO}) = 726 \text{ cm}^{-1}$ ]. The extrapolated value at ambient pressure for this mode is  $717 \text{ cm}^{-1}$ , which shows a reasonable agreement with the IR-active mode considering its broad and weak nature.

X-ray diffraction patterns have been measured at CHESS to 58 GPa at 300 K without laser heating. Below 15 GPa, no significant change in diffraction patterns was found and all diffraction lines were well fitted with those of the corundum structure ( $R\bar{3}c$ ) [Fig. 5(a)]. However, above 30 GPa, some peaks are selectively broadened: the full width at half maximum (FWHM) of  $(110)_H$  and  $(116)_H$  is a factor of 3 and FWHM of  $(104)_H$  and  $(024)_H$  is a factor of 2 greater than that of  $(012)_H$  diffraction line. In addition, systematic errors were found above 30 GPa in unit-cell parameter refinements

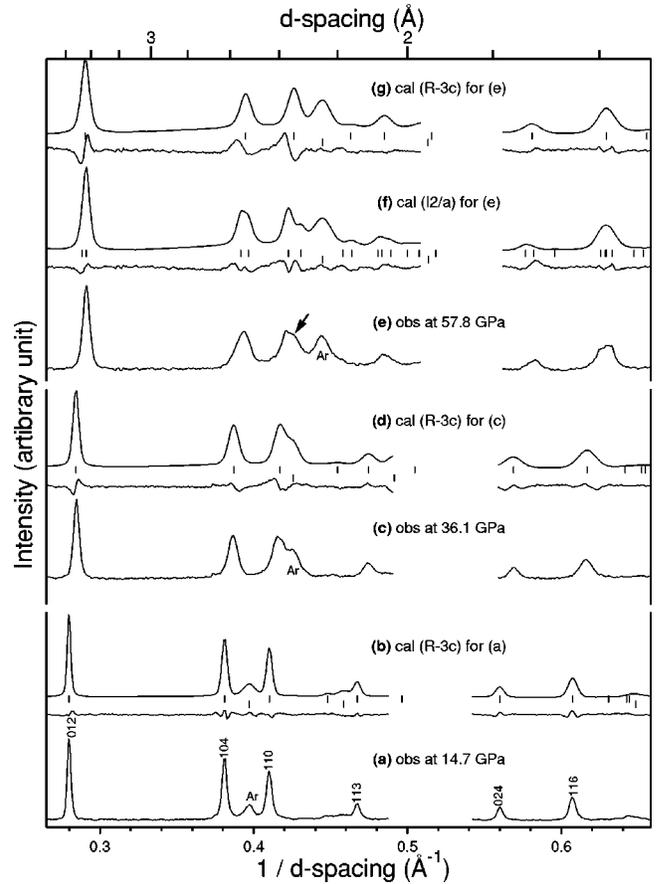


FIG. 5. Observed (a,c,e) and calculated (b,d,f,g) x-ray diffraction patterns at high pressure. The difference between the observed and calculated patterns is also shown for each calculated pattern. Tick marks are the diffraction peak positions for  $\text{Cr}_2\text{O}_3$  [corundum phase at the top of (b), (d), and (g); monoclinic  $\text{V}_2\text{O}_3$  phase at the top of (f)] and Ar [bottom of (b), (d), (f), (g)]. Backgrounds were subtracted. Hexagonal Miller indices are given for the major lines of  $\text{Cr}_2\text{O}_3$  for the pattern measured at 14.7 GPa (a). For the observed pattern at 57.8 GPa (e), we show two different refinements with the corundum-type ( $R\bar{3}c$ ) (g) and the monoclinic  $\text{V}_2\text{O}_3$ -type ( $I2/a$ ) (f) structures. The arrow indicates the peak splitting.

when the corundum-type structure is assumed. The maximum errors occurred for  $(110)_H$  and  $(116)_H$  which are the broadest lines above 15 GPa and this increases with compression. At the maximum pressure (58 GPa), we were able to observe a peak splitting of the  $(110)_H$  line [Fig. 5(e)].

We performed Rietveld refinements with two different crystal structure models (corundum type,  $R\bar{3}c$ , and monoclinic  $\text{V}_2\text{O}_3$  type,  $I2/a$ ) for the entire x-ray data set measured without laser heating. Below 15 GPa, the corundum type fits well the observed diffraction patterns. However, systematic differences were found between the calculated and observed intensities above 30 GPa after the refinements with the corundum structure: the corundum type predicts lower  $d$  spacings for  $(012)_H$  and higher  $d$  spacings for  $(104)_H$  and  $(110)_H$  than the observed patterns [Figs. 5(b), 5(d), and 5(g)]. This is the same trend observed in the unit-cell refinements for individual peak fitting results. However, use of the monoclinic

$V_2O_3$  structure decreases the systematic differences between the observed and calculated diffraction patterns, and the difference is much more random [Fig. 5(f)].

We also examined the  $Rh_2O_3$ -II-type structure ( $Pbna$ ), which is proposed by first principles calculations for a high-pressure phase of  $Cr_2O_3$  (Refs. 10 and 11), and the perovskite structure ( $Pbnm$ ), which is proposed as a high-pressure phase of  $Fe_2O_3$  (Ref. 33), by calculating diffraction patterns at corresponding pressures. However, neither of these structures are consistent with the observed subtle changes. Indeed, the observed diffraction patterns after laser heating above 30 GPa, which can be well explained by an orthorhombic unit cell, demonstrate that the diffraction pattern of the orthorhombic phase is considerably different from the observed diffraction patterns above 15–30 GPa without laser heating (see Sec. III B).

The unit-cell parameters obtained from Rietveld refinements were plotted in Fig. 6. To facilitate direct comparison, we transformed the trigonal and monoclinic cell parameters to hexagonal and pseudohexagonal cell parameters, respectively (the transformation matrix can be found in Ref. 5). Below 15 GPa, our refinement results with the trigonal lattice (corundum structure) agree well with previous studies.<sup>13,26,34</sup> However, above 30 GPa, our results for both trigonal cell and monoclinic cell refinements start to deviate from the extrapolation of hydrostatic compression data measured at lower pressure<sup>26,27</sup> and other measurements to 32 GPa (Ref. 13). However, the experiments of Refs. 13 and 34 were performed without any pressure medium (e.g., nonhydrostatic conditions) and hence are of lower quality. Our results are in reasonable agreement with Ref. 12 especially when one notes that they report anomalous values of the lattice parameters above 30 GPa which require an increase in unit-cell volume for the corundum structure. Above 30 GPa, the  $a$  axis is larger than static compression measurements at lower pressure<sup>26</sup> using the trigonal fitting by 0.7–2.7%. For the monoclinic fitting, the two pseudohexagonal  $a$  axes are no longer identical and behave differently: one axis is close to previous studies (0.1–1.6% larger) but the other axis is 1.0–3.7% larger. Except for Ref. 34, previously reported  $c$  axis shows good agreement below 15 GPa. However, above 20 GPa the difference in the  $c$  axis from the extrapolation of lower pressure measurement<sup>26</sup> is generally greater than that in the  $a$  axis: 1.4–3.7% for trigonal fits and 1.8–4.2% for monoclinic fits. After the phase transition, the  $Cr_2O_3$  structure becomes less compressible along both the  $c$  and  $a$  axes of pseudohexagonal lattice.

It has been known that the  $c/a$  ratio for the corundum-type transition-metal oxides is sensitive to physical property changes.<sup>3,4,35</sup> Below 30 GPa, our  $c/a$  ratio in  $Cr_2O_3$  is slightly higher than those of other studies but still in agreement within the experimental scatter (Fig. 7). However, above 30 GPa we observed a 0.4% increase of the  $c/a$  ratio for trigonal fits, and 0.5% and 1.5% increase for monoclinic fits. For the monoclinic case, the two  $c/a$  ratios diverge with compression.

Since the monoclinic phase and the  $c/a$  ratio change were also observed in the pure and Cr-doped  $V_2O_3$  systems and  $Cr_2O_3$  forms a complete solid solution with  $V_2O_3$  (Ref. 36),

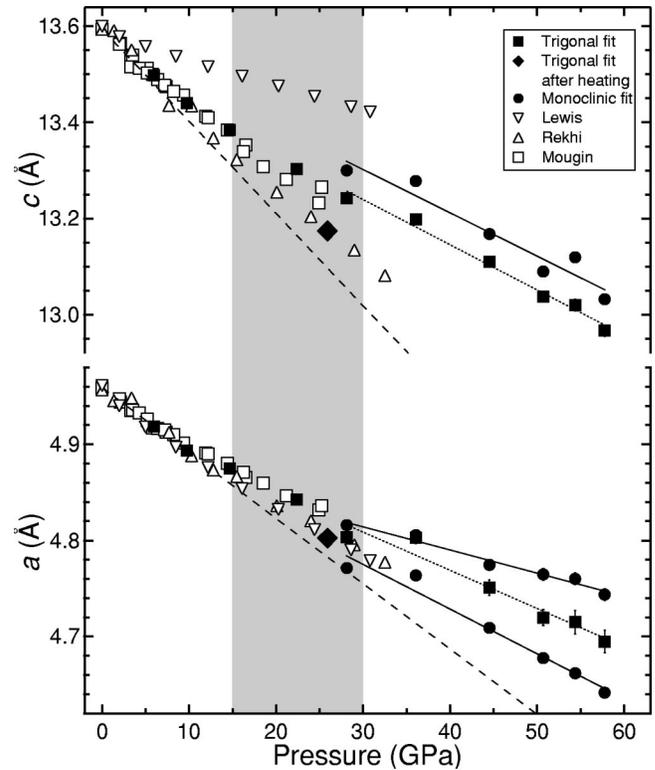


FIG. 6. Pseudohexagonal unit-cell parameters of  $Cr_2O_3$  at high pressure. Trigonal (solid squares) and monoclinic (solid circles) unit-cell parameters were transformed to pseudohexagonal unit-cell parameters to facilitate comparison. Error bars represent  $1\sigma$  uncertainty. Linear fits for results from monoclinic cell refinements (solid lines) and trigonal cell refinements (dotted lines) are shown. A trigonal fit result for the diffraction pattern measured after laser heating at 25.9 GPa is plotted (solid diamonds). The data points from previous studies (Refs. 12, 13, and 34) are also shown for comparison. Dashed lines are the extrapolation of linear fits for unit-cell parameters measured under hydrostatic stress condition (Ref. 26) below 10 GPa. Due to a severe peak overlap between  $Cr_2O_3$  and argon [ $Cr_2O_3(110)_H + Ar(111)$  and  $Cr_2O_3(113)_H + Ar(200)$ ], only trigonal fit results are shown at 15–27 GPa.

it may be reasonable to compare the current observation with the behavior of the pure and Cr-doped  $V_2O_3$  systems. In pure and Cr-doped  $V_2O_3$ , the  $c/a$  ratio increase is known to be associated with an insulator-to-metal transition: an antiferromagnetic insulator-to-metal transition at 150 K and ambient pressure in  $V_2O_3$ , and a paramagnetic insulator-to-metal transition at 1.1 GPa and 300 K in 4% Cr doped  $V_2O_3$  (Ref. 4). In fact, this systematic trend is also found in  $Ti_2O_3$ : a semiconductor-to-metal transition at 390–470 K is accompanied by a 2.1% (from 2.646 to 2.701)  $c/a$  ratio increase<sup>3</sup> with temperature. It has been proposed that relative contraction along the pseudohexagonal  $a$  axis leads to the formation of bonds between cations in the  $(001)_H$  plane of the corundum lattice, resulting in a decrease of resistivity.<sup>2,37</sup> In our study, the  $c/a$  ratio increases in  $Cr_2O_3$  at 25–30 GPa (0.4% for the trigonal cell refinement, and 2.0% and 0.5% for the monoclinic refinement).

However, it should be mentioned that the crystal structure

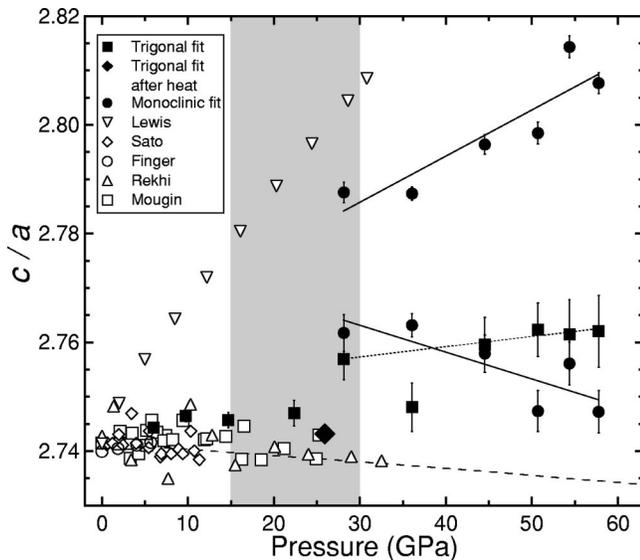


FIG. 7. The  $c/a$  ratio of  $\text{Cr}_2\text{O}_3$  at high pressure. Notations are the same as in Fig. 6. For comparison, we also show the data from lower pressure measurements (Refs. 12, 13, 26, 27, and 34). A data point at 36 GPa from trigonol fit was not included in the linear fit for the  $c/a$  vs pressure (dotted line). Due to a severe peak overlap between  $\text{Cr}_2\text{O}_3$  and argon [ $\text{Cr}_2\text{O}_3(110)_H + \text{Ar}(111)$  and  $\text{Cr}_2\text{O}_3(113)_H + \text{Ar}(200)$ ], only trigonol fits are shown at 15–27 GPa.

change from the monoclinic to the trigonal in  $\text{V}_2\text{O}_3$  was observed together with the increase of the  $c/a$  ratio, which is the opposite of our observation for  $\text{Cr}_2\text{O}_3$  at high pressure. The driving force in  $\text{V}_2\text{O}_3$  is a contraction of structure along the  $c$  axis and an elongation along the  $a$  axis, while in  $\text{Cr}_2\text{O}_3$  it occurs in the opposite fashion. Thus, it may not be appropriate to use the increase of the  $c/a$  ratio in  $\text{Cr}_2\text{O}_3$  as a sign of an insulator-metal transition.

The volume change in  $\text{Cr}_2\text{O}_3$  at high pressure is shown in Fig. 8. Our measurement is consistent with recent x-ray diffraction experiments<sup>12</sup> and slightly higher than the extrapolation of low-pressure hydrostatic measurements.<sup>26</sup> We do not observe a discrete change in volume of any significance, within the observed data scatter, during cold compression for the entire pressure range we studied at 300 K. A recent measurement<sup>12</sup> reported that  $\text{Cr}_2\text{O}_3$  becomes almost incompressible above 30 GPa. Our data points at 28–36 GPa can be interpreted as being consistent with this observation. However, the change at 28–36 GPa is still within the observed scatter of the data points (Fig. 8). Due to the expected subtle nature of the transition to the monoclinic  $\text{V}_2\text{O}_3$ -type phase and the finite resolution of the high-pressure technique we used, it is difficult to detect the phase transition pressure using the volume data.

### B. Phase transition above 30 GPa and high temperature

Drastic changes in Raman spectra were observed after laser heating above 30 GPa (Fig. 9). After heating, wave numbers of Raman modes are different from those observed before heating, and the number of observed modes increases

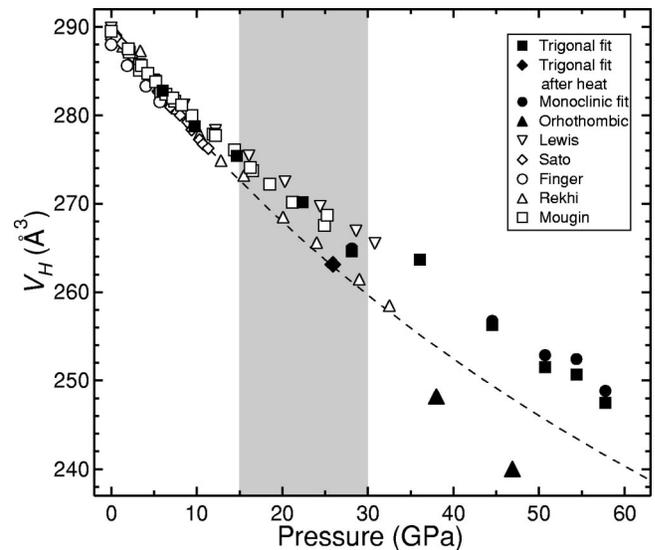


FIG. 8. Volume of  $\text{Cr}_2\text{O}_3$  transformed to pseudohexagonal unit cell ( $Z=6$ ) at high pressure. Notations are the same as in Fig. 7. The volume of the orthorhombic phase observed after laser heating at 38 and 46.9 GPa is also shown (solid triangles). Dashed curve is the extrapolation of hydrostatic compression (Ref. 26) below 10 GPa at 300 K ( $K_{T0}=222$  GPa and  $K'_{T0}=4$ ). Due to a severe peak overlap between  $\text{Cr}_2\text{O}_3$  and argon [ $\text{Cr}_2\text{O}_3(110)_H + \text{Ar}(111)$  and  $\text{Cr}_2\text{O}_3(113)_H + \text{Ar}(200)$ ], only trigonol fits are shown at 15–27 GPa.

from 9 to 12 (Fig. 10). The latter could mean a structural change to a lower symmetry phase: according to group theory, a total of 24 modes for the perovskite type and 30 modes for the  $\text{Rh}_2\text{O}_3$ -II type are expected to be Raman ac-

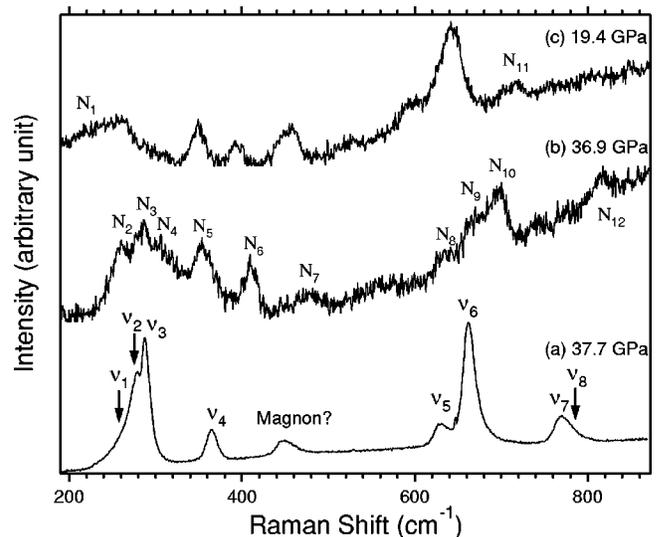


FIG. 9. High-pressure Raman spectra of  $\text{Cr}_2\text{O}_3$  measured after laser heating (b) and after decompression of the laser-heated sample (c). Raman spectrum without laser heating measured at 37.7 GPa is shown for comparison. New features observed after laser heating at 36.9 GPa are named in sequential order starting from the lowest wave-number peak ( $N_1$ – $N_{12}$ ). New features observed above 15–30 GPa during cold compression are indicated by arrows ( $v_1$ ,  $v_2$ , and  $v_8$ ). Pressure is shown above each trace.

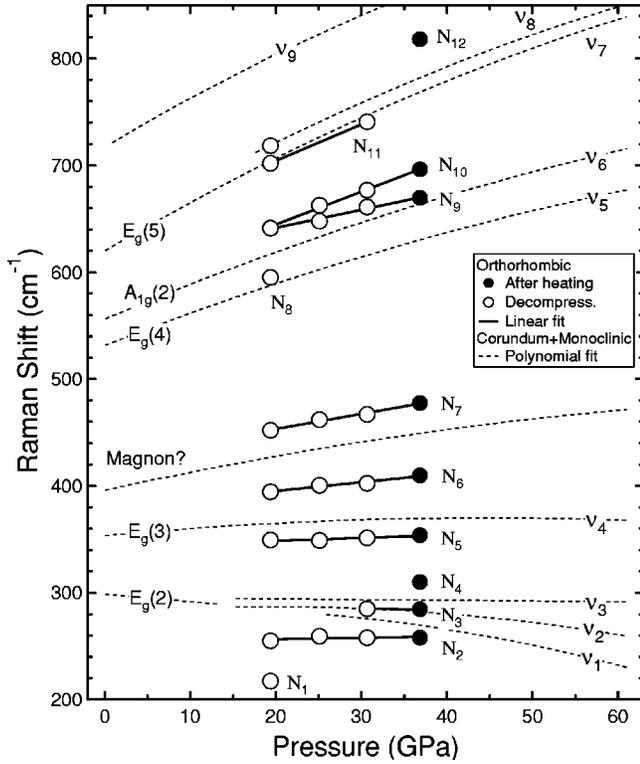


FIG. 10. Pressure shift of Raman modes for the orthorhombic phase of  $\text{Cr}_2\text{O}_3$ . Solid circles are the data points measured after laser heating and open circles are the data points measured during decompression of the laser heated sample. Linear fits for data points are shown as solid lines. For comparison, the positions of Raman modes of the corundum and the monoclinic  $\text{V}_2\text{O}_3$ -type  $\text{Cr}_2\text{O}_3$  are shown as dotted lines using the polynomial fits presented in Fig. 3. Peak assignments are the same as in Fig. 1.

tive, whereas only 7 for the corundum type and 15 for the monoclinic  $\text{V}_2\text{O}_3$  type are expected to be Raman active. However, as shown for the orthorhombic phase of  $\text{Fe}_2\text{O}_3$  above 55 GPa, not all Raman-active modes are observable.<sup>7</sup> In addition, Raman scattering becomes much weaker after heating. It is interesting that decreases in Raman scattering intensities were also observed for the phase transition in  $\text{Fe}_2\text{O}_3$  at 55 GPa (Ref. 7).

Many of the modes appearing after laser heating (solid circles in Fig. 10) still remain during decompression (open circles in Fig. 10). However, the wave numbers for some modes coincide with those of the modes observed without heating ( $N_1$ ,  $N_8$ , and  $N_{11}$  in Fig. 10). Since Raman scattering was much more intense before heating, a small amount of the back-transformed material could show scattering with significant intensities.

Considerable changes were also observed in diffraction patterns after laser heating (Fig. 11): new diffraction lines appear at 3.0, 2.4, and 1.7 Å and intensities of the low  $d$ -spacing lines change significantly. However, some major diffraction lines of the low-temperature phase (either the corundum or the monoclinic  $\text{V}_2\text{O}_3$  type) still persist even after laser heating, i.e., diffraction lines at 3.4 and 2.75 Å. This implies that the phase transition to this orthorhombic phase is very sluggish.

The observed diffraction patterns after laser heating can be well explained by an orthorhombic unit cell. We also performed Rietveld analyses for the diffraction patterns of the orthorhombic phase. We used both the  $\text{Rh}_2\text{O}_3$ -II type ( $Pbna$ ,  $D_{2h}^{14}$ ) and the perovskite-type ( $Pbnm$ ,  $D_{2h}^{16}$ ) structures as starting models for the analyses. Refinements with both of these models show equally good fit to the peak positions observed after laser heating. However, when we release the constraints for atomic positions in Rietveld analyses, we found very anisotropic Cr-O polyhedra for both the space groups: maximum 42% difference of Cr-O bonds in the octahedra of the  $\text{Rh}_2\text{O}_3$ -II type and maximum 35% difference for Cr-O bonds in the dodecahedra of the perovskite type (we considered nearest eight oxygens, since the perovskite structure with  $Pbnm$  space group inherently has distorted dodecahedra such that eight oxygens are closely coordinated around a Cr atom).

These values are rather extreme compared with the reported anisotropy of polyhedra in these structures. For example, for the  $\text{Rh}_2\text{O}_3$ -II-type structures, 5% and 10% anisotropies of octahedra are reported in  $\text{Rh}_2\text{O}_3$  (Ref. 38) and  $\text{Fe}_2\text{O}_3$  (Ref. 39) at high pressure, respectively. In the perovskite-type structures, 22% and 21% anisotropies of dodecahedra are reported in  $\text{GdFeO}_3$  (Ref. 40) and  $\text{MgSiO}_3$  (Ref. 41) perovskites at ambient pressure, respectively. Thus, the obtained atomic positions for the orthorhombic phase may not be realistic. In fact, for the measurements with laser heating, we used a slot-type aperture of Mao-Bell-type diamond cell. This allows only  $8^\circ$ – $10^\circ$  arc of diffraction rings. Furthermore, recrystallization and preferred orientation induced during laser heating can decrease the accuracy of the measured intensity considerably.<sup>42</sup> These pose severe limits in determination of atomic positions using the measured intensity.

We also performed refinements with quasirigid body constraints for Cr-O polyhedra in the structures: we set limits in the variations of Cr-O bond lengths. For the same allowed variations, the weighted residual factor  $R_{wp}$  is slightly better when the perovskite type is used, but the difference is less than 0.2%. For space-group determination, more precise measurements for diffraction intensities are required.

We compare the volume of the orthorhombic phase with those of the corundum and the monoclinic  $\text{V}_2\text{O}_3$ -type phases (Fig. 8). Compared with the compressional curve extrapolated from low-pressure measurements,<sup>26</sup> the orthorhombic structure decreases volume by 2–3%, whereas the volume decrease is 5–6%, if compared with that of the monoclinic  $\text{V}_2\text{O}_3$ -type phase. The volume decrease for the corundum-to- $\text{Rh}_2\text{O}_3$ -II transition is reported to be 3.2% for  $\text{Rh}_2\text{O}_3$  (Ref. 38) and 10% for  $\text{Fe}_2\text{O}_3$  (Ref. 39).

#### IV. DISCUSSION

We observed the sample at each pressure step during Raman and x-ray experiments using an optical microscope. At ambient pressure,  $\text{Cr}_2\text{O}_3$  has a green color. It becomes darker with compression and turns to dark red near 14 GPa. Above 30 GPa after laser heating, the sample color changed from dark red to dark green. However, below 30 GPa, the sample

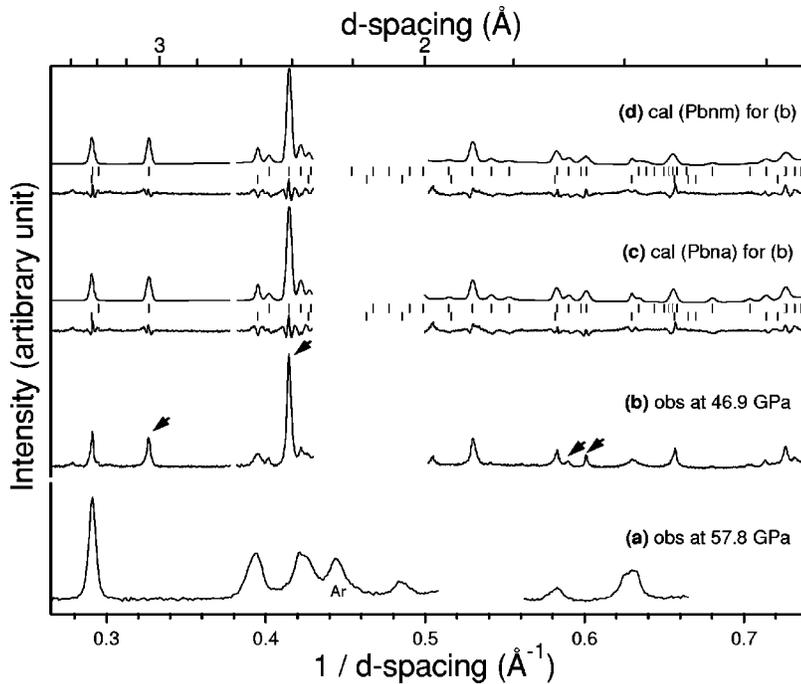


FIG. 11. Observed (a,b) and calculated (c,d) x-ray diffraction patterns at high pressure. The difference between the observed and calculated patterns is also shown for each calculated pattern. Tick marks are the diffraction peak positions for  $\text{Cr}_2\text{O}_3$  [monoclinic  $\text{V}_2\text{O}_3$  phase at the bottom of (c) and (d); orthorhombic phase at the top of (c) and (d)]. Backgrounds were subtracted. For comparison, the observed pattern at 57.8 GPa is shown in (a). Two different refinements with the  $\text{Rh}_2\text{O}_3$ -II-type ( $Pbna$ ) (c) and the perovskite-type ( $Pbnm$ ) (d) structures are shown for the pattern measured at 46.9 GPa after laser heating (b). The data points at  $0.378\text{--}0.382\text{ \AA}^{-1}$  and  $0.430\text{--}0.502\text{ \AA}^{-1}$  were not used in the refinements due to the overlaps with gasket peaks. The arrows indicate distinct major diffraction features of the orthorhombic phase.

still shows a dark red color even after laser heating. These visual observations, together with Raman scattering and x-ray diffraction, show that there exist changes in the compressional behavior of  $\text{Cr}_2\text{O}_3$  at high pressure.

Colors in  $3d$ -transition metal sesquioxides are related to the crystal-field splitting of their  $3d$  orbitals.<sup>43</sup> This splitting depends on cation-anion bond lengths and symmetry of the cation site. In an ideal octahedron, degenerated  $d$ -orbitals split into  $t_{2g}$  and  $e_g$  orbital groups energetically. The energy separation of these,  $\Delta$ , can be expressed as a function of average cation-anion separation  $R$ ,

$$\frac{\Delta}{\Delta_0} = \left(\frac{R_0}{R}\right)^5, \quad (2)$$

assuming that there is no change in the symmetry of the octahedron. Using this relation, we calculated an average cation-anion separation needed for  $\text{Cr}_2\text{O}_3$  to show same  $\Delta$  as ruby ( $\Delta = 18\,150\text{ cm}^{-1}$ , Ref. 44). For  $\Delta_0 = 16\,670\text{ cm}^{-1}$  (Ref. 45) and  $R_0 = 1.986\text{ \AA}$ , we obtained  $R = 1.952\text{ \AA}$ . This corresponds to the Cr-O length at 14 GPa where the color change from green to red is observed [Fig. 12(a)], implying that the color change is induced by the compression of  $\text{CrO}_6$  octahedra.

However, the color of  $\text{Cr}_2\text{O}_3$  changes back to green after laser heating above 30 GPa. We found that average Cr-O distance increases when  $\text{Cr}_2\text{O}_3$  transforms to the orthorhombic phase. If ruby transforms from the corundum structure to the orthorhombic structure above 100 GPa as predicted<sup>8,9</sup> and the phase transition is similar to that in  $\text{Cr}_2\text{O}_3$  as proposed by the first-principles study,<sup>10</sup> this discrete change in crystal-field energy during the phase transition to the orthorhombic phase could result in a significant change in the ruby scale.

In order to further investigate the source of the crystal structure change, we plot measured Cr-O and O-O bond

lengths as a function of pressure (Fig. 12). These values are obtained from Rietveld analyses of the diffraction patterns measured at high pressure and 300 K, with and without laser annealing, using the corundum structure. The monoclinic  $\text{V}_2\text{O}_3$  structure can be thought as a distorted corundum structure with small differences including the absence of three-fold axes along the  $c$  axis of the trigonal unit cell in the monoclinic structure. Unfortunately, our diffraction experiments do not cover sufficient reciprocal space to refine the individual oxygen positions in the monoclinic structure. Thus, we use the results from the refinements with the corundum structure, which has only one atomic position parameter to be refined for oxygen, instead in the monoclinic  $\text{V}_2\text{O}_3$  structure four oxygen position parameters should be refined. Use of these results may lead to systematic errors in the measured bond lengths above 30 GPa where significant misfits of the observed diffraction patterns with the corundum structure are observed (Fig. 5). However, the misfits are not significant below 30 GPa. Also the observed trend is still preserved even after laser heating near 30 GPa [diamond symbols in Figs. 12(a) and 12(c)] where differential stress should be much smaller. In addition, the trends observed in our data are very consistent with that observed in single-crystal diffraction experiments<sup>27</sup> below 6 GPa [Fig. 12(a)].

Oxygens in the corundum structure are hexagonally close packed. Two-thirds of the octahedral interstitial sites are filled with cations and one-third of the sites remain empty. Along the  $c$  axis, two cation-filled octahedra share one oxygen plane (“shared” by two cations above and below; represented by subscript “ $s$ ”) and one empty octahedron shares an oxygen plane with one filled octahedron (“unshared”; represented by subscript “ $u$ ”). At ambient pressure,  $M\text{-O}_s$  ( $M$ : cation,  $M = \text{Al, V, Cr, Fe}$ ) is longer than  $M\text{-O}_u$ . However, in both single-crystal and our powder-diffraction measurements, the  $\text{Cr-O}_s$  bond length decreases rapidly with

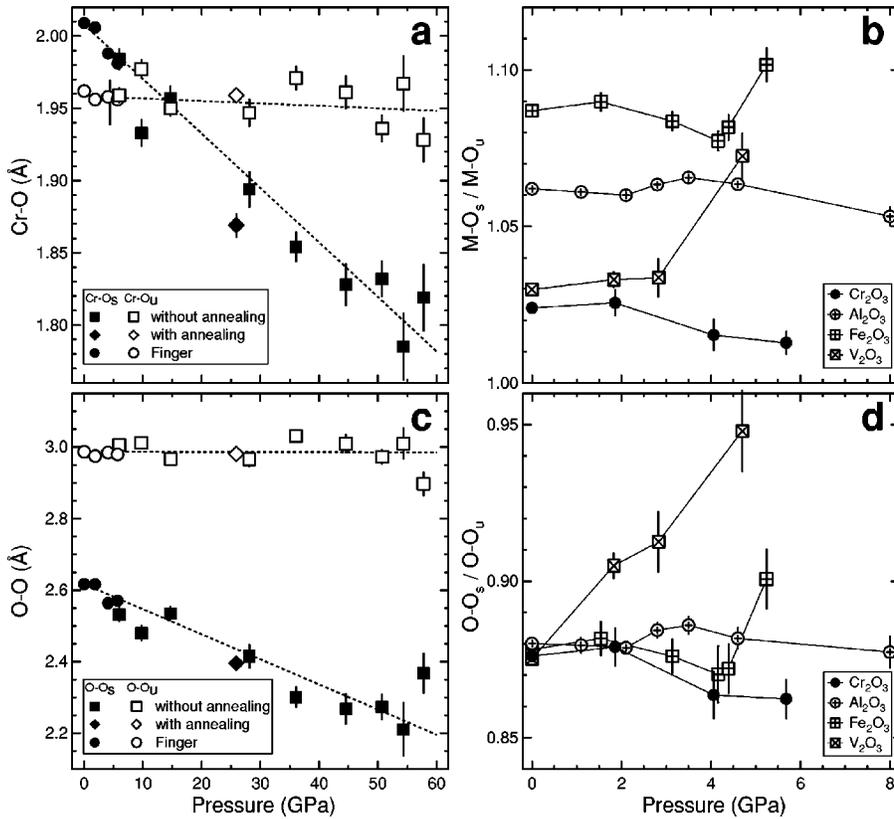


FIG. 12. (a) Cr-O and (c) O-O bond lengths in the corundum-type  $\text{Cr}_2\text{O}_3$  measured at high pressure and 300 K. Bond lengths between Cr and O in both shared (subscript “s,” solid symbols) and unshared (subscript “u,” open symbols) oxygen layers are shown for measurements both with (diamonds) and without (squares) laser annealing. The measured values by a single-crystal x-ray diffraction (Ref. 27) are also plotted for comparison (circles). We compared (b) cation-oxygen ( $M\text{-O}$ ) and (d) oxygen-oxygen ( $\text{O-O}$ ) bond length ratios between oxygens in shared and unshared oxygen planes in different corundum-type sesquioxides at high pressure and 300 K. The values are obtained from single-crystal x-ray-diffraction measurements (Refs. 46 and 27).

compression, whereas  $\text{Cr-O}_u$  is very insensitive to compression. In fact, these two Cr-O bond lengths are almost identical near 15 GPa and the  $\text{Cr-O}_s$  bond length becomes smaller than the  $\text{Cr-O}_u$  bond length above 20 GPa. Although it is difficult to see the trend in single-crystal diffraction measurements due to their limited pressure range, the decrease of the  $M\text{-O}_s$  bond length relative to the  $M\text{-O}_u$  bond length can be found in the data for  $\text{Cr}_2\text{O}_3$  [Fig. 12(b)].

In the corundum structure, cations are not at the center of octahedra, instead they are offset from the center along the  $c$  axis. Thus, the shift of Cr with compression toward the shared oxygen plane could result in the observed decrease in  $\text{Cr-O}_s$ . However, as shown in Fig. 12(c), it is the decrease of the O-O bond length in the shared oxygen plane, i.e., decrease in the size of the plane, that gives rise to the decrease in  $\text{Cr-O}_s$  bond length. In other words, the shift of oxygens in the shared plane towards the center of the triangle results in the decrease in  $\text{Cr-O}_s$  bond length. Interestingly, the size of the unshared oxygen plane is very insensitive to pressure. Also this relative decrease in  $\text{O-O}_s$  bond length can be seen in single-crystal diffraction measurements [Fig. 12(d)].

Recent first-principles calculations<sup>10,11</sup> have proposed that  $\text{Cr}_2\text{O}_3$  will show a similar phase transition to that in  $\text{Al}_2\text{O}_3$  at much lower pressure. It is difficult to compare the pressure behavior of bond lengths in  $\text{Al}_2\text{O}_3$  with those in  $\text{Cr}_2\text{O}_3$ , since only a single-crystal x-ray diffraction measurement with a limited pressure range is available. However, Fig. 12(b) and 12(c) show that the bond lengths in  $\text{Al}_2\text{O}_3$  follow a more or less similar trend to those in  $\text{Cr}_2\text{O}_3$ . In contrast,  $\text{Fe}_2\text{O}_3$  and  $\text{V}_2\text{O}_3$  show opposite pressure behaviors in bond lengths.

It is interesting that there is difference in transition pressures detected by Raman scattering and x-ray diffraction for the corundum-to-monoclinic  $\text{V}_2\text{O}_3$  phase transition: whereas two new Raman modes are observed from 15 GPa (Fig. 3), the  $c/a$  ratio measured by x-ray diffraction shows a discrete increase at 25–28 GPa (Fig. 7). It should be noted that the expected changes in the phase transition are subtle. Furthermore, we have a finite resolution in both Raman and x-ray-diffraction measurements, due to stress inhomogeneity, non-hydrostatic stresses, and so on. In fact, the two new modes ( $\nu_2$  and  $\nu_8$  in Fig. 3) are not fully resolved to 30 GPa and these appear only as asymmetry of modes  $\nu_3$  and  $\nu_7$ . Furthermore,  $\nu_1$  is resolved above 30 GPa which is rather close to where the  $c/a$  ratio change is found in diffraction experiments.

We also investigated whether the monoclinic  $\text{V}_2\text{O}_3$  phase is induced by nonhydrostatic stresses in the sample. In fact, there is some evidence for the existence of differential stresses in our experiments: the volume measured without laser annealing above 15 GPa is 1% higher than that extrapolated from low-pressure hydrostatic experiments<sup>26</sup> and that measured after annealing at 26 GPa (Fig. 8). Also, the FWHM of diffraction peaks measured during cold compression is significantly larger than that measured after laser annealing (Fig. 11). In contrast, the bond distance change (Fig. 12) in an annealed sample at 26 GPa is in good agreement with those in cold compressed samples, and the Raman features observed before annealing are still preserved after annealing at 26 GPa. A measurement with quasihydrostatic medium, e.g., helium, is warranted to resolve this issue. The

monoclinic  $V_2O_3$ -type phase is metastable above 30 GPa where a 5–6% more dense phase, the orthorhombic phase, exists (Fig. 8).

## V. CONCLUSION

We have observed a color change, splittings of Raman modes, relative increases of some Raman mode intensities, selective broadening of some diffraction lines, and systematic shifts of some diffraction positions in  $Cr_2O_3$  at 15–30 GPa. The Raman spectrum and diffraction changes are consistent with a phase transition to the monoclinic  $V_2O_3$  structure ( $I2/a$ ), which has also been observed in pure and Cr-doped  $V_2O_3$  systems, but the observed changes are not consistent with a phase transition to the orthorhombic structure ( $Rh_2O_3$ -II or perovskite type). The phase transition may be induced by the different compressibility of cation-filled and empty octahedra in  $Cr_2O_3$ .

We also find another phase transition above 30 GPa and after laser heating. The high-temperature phase has an orthorhombic unit cell as predicted by first-principles calculations<sup>10</sup> and Rietveld refinement shows that this could be either the  $Rh_2O_3$ -II or the perovskite-type structure. The

color change during this phase transition, from dark red to green, is consistent with the fact that average Cr-O bond length increases after the phase transition. Since the orthorhombic phase has much smaller volume than the monoclinic  $V_2O_3$ -type phase, the orthorhombic phase is more stable than the monoclinic phase above 30 GPa. It is interesting that the monoclinic  $V_2O_3$ -type phase survives metastably over a wide pressure range (30–60 GPa).

Since it has been proposed that the phase transition in  $Cr_2O_3$  is similar to that expected in ruby,<sup>10,11</sup> the phase transitions found in this study may have important implications for the ruby scale. This study shows that the phase transitions in  $Cr_2O_3$  are accompanied with changes in both cation-anion bond length and cation site symmetry, which are important factors to influence the crystal-field splitting energy whose pressure variation is used in the ruby scale.

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- <sup>1</sup>P. A. Cox, *Transition Metal Oxides—an Introduction to their Electronic Structure and Properties*, International Series of Monographs on Chemistry Vol. 27 (Oxford Science Publications, Oxford, 1992).
- <sup>2</sup>A. Mooradian and P.M. Raccach, *Phys. Rev. B* **3**, 4253 (1971).
- <sup>3</sup>C.N.R. Rao, R.E. Loehman, and J.M. Honig, *Phys. Lett.* **27A**, 271 (1968).
- <sup>4</sup>D.B. McWhan and J.P. Remeika, *Phys. Rev. B* **2**, 3734 (1970).
- <sup>5</sup>P.D. Dernier and M. Marezio, *Phys. Rev. B* **2**, 3771 (1970).
- <sup>6</sup>M.P. Pasternak, G.K. Rozenberg, G.Y. Machavariani, O. Naaman, R.D. Taylor, and R. Jeanloz, *Phys. Rev. Lett.* **82**, 4663 (1999).
- <sup>7</sup>S.-H. Shim and T.S. Duffy, *Am. Mineral.* **87**, 318 (2002).
- <sup>8</sup>K.T. Thomson, R.M. Wentzcovitch, and M.S.T. Bukowinski, *Science* **274**, 1880 (1996).
- <sup>9</sup>N. Funamori and R. Jeanloz, *Science* **278**, 1109 (1997).
- <sup>10</sup>W. Duan, G. Paiva, R.M. Wentzcovitch, and A. Fazzio, *Phys. Rev. Lett.* **81**, 3267 (1998).
- <sup>11</sup>A.Y. Dobin, W. Duan, and R.M. Wentzcovitch, *Phys. Rev. B* **62**, 11 997 (2000).
- <sup>12</sup>J. Mougín, T.L. Bihan, and G. Lucazeau, *J. Phys. Chem. Solids* **62**, 553 (2001).
- <sup>13</sup>S. Rekhí, L.S. Dubrovinsky, R. Ahuja, S.K. Saxena, and B. Johansson, *J. Alloys Compd.* **302**, 16 (2000).
- <sup>14</sup>H.-K. Mao, J. Xu, and P.M. Bell, *J. Geophys. Res.* **91**, 4673 (1986).
- <sup>15</sup>L.W. Finger, R.M. Hazen, G. Zou, H.-K. Mao, and P.M. Bell, *Appl. Phys. Lett.* **39**, 892 (1981).
- <sup>16</sup>S. Desgreniers, University of Ottawa, Technical Report, 1998 (unpublished).
- <sup>17</sup>T.J.B. Holland and S.A.T. Redfern, *Miner. Mag.* **61**, 65 (1997).
- <sup>18</sup>A. C. Larson and R. B. V. Dreele, Los Alamos National Laboratory, Technical Report No. LAUR 86-748, 1988 (unpublished).

- <sup>19</sup>G. Shen, M.L. Rivers, Y. Wang, and S.R. Sutton, *Rev. Sci. Instrum.* **72**, 1273 (2001).
- <sup>20</sup>I.R. Beattie and T.R. Gilson, *J. Chem. Soc. A* **5**, 980 (1970).
- <sup>21</sup>T. R. Hart, R. L. Aggarwal, and B. Lax, in *Proceedings of the Second International Conference on Light Scattering in Solids*, edited by M. Balkanski (Flammarion Sciences, Paris, 1971), pp. 174–179.
- <sup>22</sup>C. Tatsuyama and H.Y. Fan, *Phys. Rev. B* **21**, 2977 (1980).
- <sup>23</sup>K.F. McCarty and D.R. Boehme, *J. Solid State Chem.* **79**, 19 (1989).
- <sup>24</sup>N. Kuroda and H.Y. Fan, *Phys. Rev. B* **16**, 5003 (1977).
- <sup>25</sup>D. Bloch, *J. Phys. Chem. Solids* **27**, 881 (1966).
- <sup>26</sup>Y. Sato and S. Akimoto, *J. Appl. Phys.* **50**, 5285 (1979).
- <sup>27</sup>L.W. Finger and R.M. Hazen, *J. Appl. Phys.* **51**, 5362 (1980).
- <sup>28</sup>M.C. Aronson, S.B. Dierker, B.S. Dennis, S.-W. Cheong, and Z. Fisk, *Phys. Rev. B* **44**, 4657 (1991).
- <sup>29</sup>V.V. Struzhkin, A.F. Goncharov, and K. Syassen, *Mater. Sci. Eng., A* **168**, 107 (1993).
- <sup>30</sup>V.V. Struzhkin, U. Schwarz, H. Wilhelm, and K. Syassen, *Mater. Sci. Eng., A* **168**, 103 (1993).
- <sup>31</sup>E.J. Samuelsen, *Physica (Amsterdam)* **43**, 353 (1969).
- <sup>32</sup>G. Lucovsky, R.J. Sladek, and J.W. Allen, *Phys. Rev. B* **16**, 4716 (1977).
- <sup>33</sup>A.F. Reid and A.E. Ringwood, *J. Geophys. Res.* **74**, 3238 (1969).
- <sup>34</sup>H.J. Lewis, Jr. and H.G. Drickamer, *J. Chem. Phys.* **45**, 224 (1966).
- <sup>35</sup>C.T. Prewitt, R.D. Shannon, D.B. Rogers, and A.W. Sleight, *Inorg. Chem.* **8**, 1985 (1969).
- <sup>36</sup>R. S. Roth, *Phase Equilibria Diagrams-Phase Diagrams for Ceramists* (The American Ceramic Society, 1995).
- <sup>37</sup>J. B. Goodenough, *Magnetism and the Chemical Bond* (Robert E. Krieger, New York, 1976).
- <sup>38</sup>R.D. Shannon and C.T. Prewitt, *J. Solid State Chem.* **2**, 134 (1970).

- <sup>39</sup>G.K. Rozenberg, L.S. Dubrovinsky, M.P. Pasternak, O. Naaman, T.L. Bihan, and R. Ahuja, *Phys. Rev. B* **65**, 064112 (2002).
- <sup>40</sup>S. Geller, *J. Chem. Phys.* **24**, 1236 (1956).
- <sup>41</sup>H. Horiuchi, E. Ito, and D.J. Weidner, *Am. Mineral.* **72**, 357 (1987).
- <sup>42</sup>S.-H. Shim, R. Jeanloz, and T.S. Duffy, *Geophys. Res. Lett.* **29**, 2166 (2002).
- <sup>43</sup>R. G. Burns, *Mineralogical Applications of Crystal Field Theory* (Cambridge University Press, New York, USA, 1993).
- <sup>44</sup>R.M. Macfarlane, *J. Chem. Phys.* **39**, 3118 (1963).
- <sup>45</sup>D.S. McClure, *J. Chem. Phys.* **38**, 2289 (1963).
- <sup>46</sup>L.W. Finger and R.M. Hazen, *J. Appl. Phys.* **49**, 5823 (1978).