

# The Effect of Salinity on the Wind-Driven Circulation and the Thermal Structure of the Upper Ocean

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## ABSTRACT

Studies of the effect of a freshening of the surface waters in high latitudes on the oceanic circulation have thus far focused almost entirely on the deep thermohaline circulation and its poleward heat transport. Here it is demonstrated, by means of an idealized general circulation model, that a similar freshening can also affect the shallow, wind-driven circulation of the ventilated thermocline and its heat transport from regions of gain (mainly in the upwelling zones of low latitudes) to regions of loss in higher latitudes. A freshening that decreases the surface density gradient between low and high latitudes reduces this poleward heat transport, thus forcing the ocean to gain less heat in order to maintain a balanced heat budget. The result is a deepening of the equatorial thermocline. (The deeper the thermocline in equatorial upwelling zones is, the less heat the ocean gains.) For a sufficiently strong freshwater forcing, the poleward heat transport all but vanishes, and permanently warm conditions prevail in the Tropics. The approach to warm oceanic conditions is shown to introduce a bifurcation mechanism for the north–south asymmetry of the thermal and salinity structure of the upper ocean.

## 1. Introduction

A salient feature of the oceanic thermal structure is the remarkably shallow, sharp, tropical thermocline that separates warm surface waters from the cold water at depth. The shallowness of the thermocline is of great importance to the earth's climate: it permits phenomena such as El Niño, which corresponds to a temporary warming of the surface waters of the eastern equatorial Pacific Ocean when the zonal slope of the equatorial thermocline decreases. At first it was thought that the maintenance of the shallow thermocline depends mainly

on the deep thermohaline circulation, which involves the sinking of cold, saline surface waters in certain high-latitude regions [for a review of various approaches see Veronis (1969)]. Robinson and Stommel (1959) assumed that the tropical thermocline remains shallow despite the downward diffusion of heat because that diffusion is countered by the upward motion of cold water from below the thermocline. Subsequently, estimates of the vertical diffusivity  $k$  on the basis of measurements (e.g., Ledwell et al. 1993) indicated that, in reality, the value of  $k$  is far smaller than the value required by the theory. This led to a reassessment of the processes maintaining the oceanic thermal structure.

Today the thermal structure of the ocean is regarded as depending not only on the deep thermohaline circulation, but also on the wind-driven circulation of the upper ocean. The latter involves asymmetrical gyres with intense western boundary currents such as the Gulf Stream and Kuroshio. The first models of these gyres (Stommel 1948) ignored the vertical structure of the

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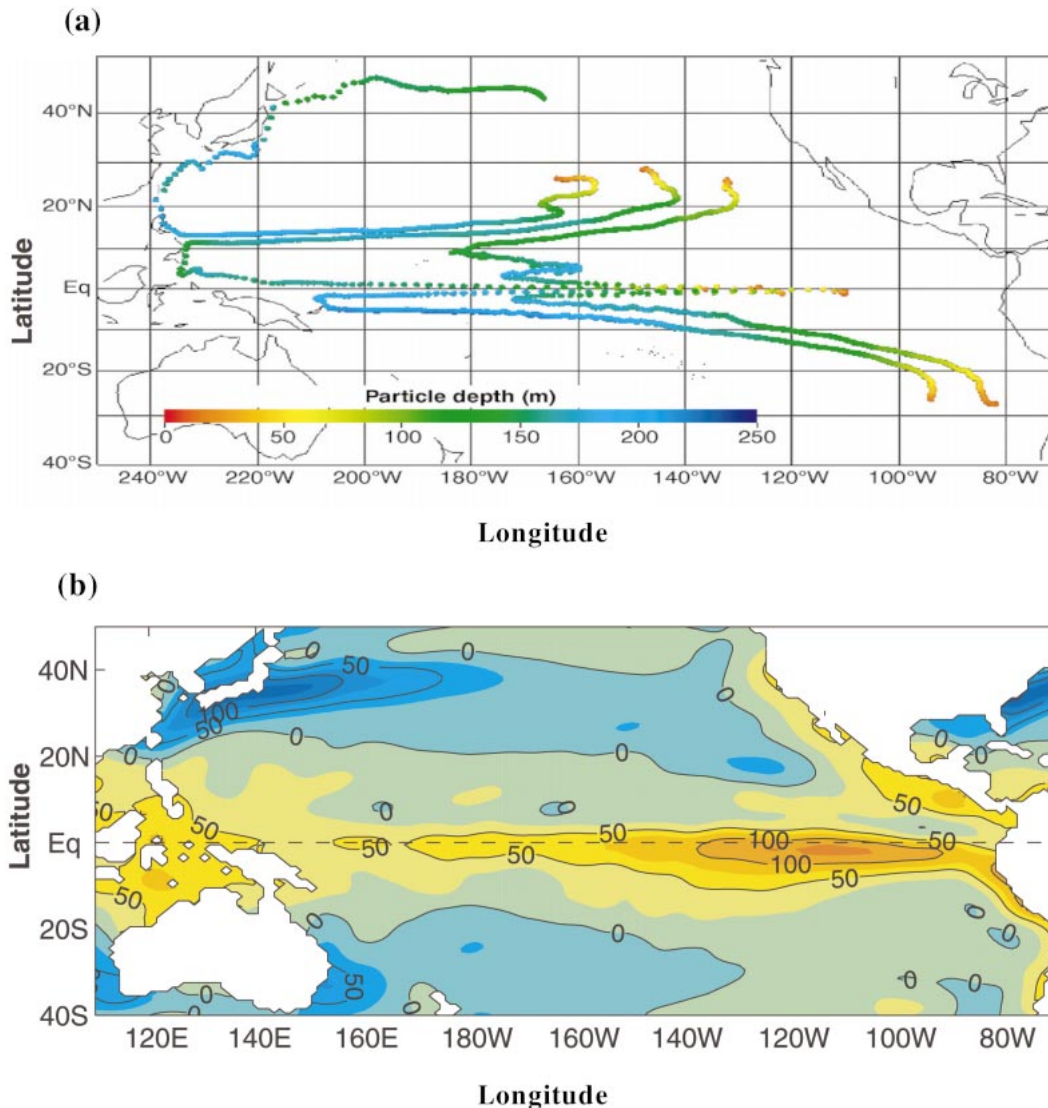


FIG. 1. (a) The wind-driven circulation of the Pacific as portrayed in the paths of sample water parcels over a period of 16 years after subduction off the coasts of California and Chile. The trajectories are from a realistic general circulation model of the ocean forced with the observed climatological winds (Harper 2000). The dots, at intervals of one month, indicate rapid motion in the Equatorial Undercurrent and Kuroshio. The colors show the depth of the water parcels, which move on the constant density surface in Fig. 2. The near-surface Ekman flow away from the equator (not shown here) closes this circulation. (b) The heat flux ( $W m^{-2}$ ) into the ocean in low latitudes and out of the ocean in higher latitudes.

flow. Montgomery (1938) and Iselin (1939) were first to introduce the concept of thermocline ventilation. Subsequently Welander (1959), Luyten et al. (1983), and Huang (1986), among others, explored the three-dimensional structure of the gyres in the presence of stratification. They developed the theory of the ventilated thermocline and identified subtropical regions of “subduction” where the winds force surface water downward whereafter motion is along surfaces of constant density. Figure 1a shows the trajectories of a few sample water parcels over a period of 16 years after subduction in a realistic general circulation model of the Pacific

Ocean (Harper 2000). Some of the water is seen to join the gyre that includes the Kuroshio. Some of the water is seen to flow to low latitudes, ultimately rising back to the surface in the equatorial upwelling zone of the eastern Pacific. The subsequent motion of the water, not shown in Fig. 1a, includes poleward drift in the surface Ekman layer until the water joins the subtropical gyre and ultimately returns to the region of subduction. This circulation, in Ekman layers at the surface, on isopycnal surfaces after subduction, effects a poleward transport of heat from the equatorial upwelling zone where the ocean gains much of its heat to higher latitudes where

the heat is lost, mainly off Japan. (The regions of gain and loss are shown in Fig. 1b, a map of heat fluxes across the ocean surface.)

The wind-driven ventilated thermocline circulation determines the thermal structure of the upper ocean in the Tropics and subtropics. It essentially maps latitudinal temperature gradients at the surface onto the vertical. It does so only for the upper ocean because, as is evident in Fig. 1a, the wind-driven circulation penetrates to a depth of a few hundred meters at most. That depth depends on the density of the deep ocean, which is maintained by the deep thermohaline circulation. Hence the ventilated thermocline depends on the thermohaline circulation. Theories for the ventilated thermocline (Pedlosky 1996) assume that, in the absence of winds, the depth  $H$  of the thermocline is given and then determine how the winds affect that depth. (Alternatively, in the presence of winds, the depth  $H$  is assumed to be known along the eastern boundary of the basin.) This free parameter  $H$  in theories for the ventilated thermocline represents the implicit presence of the thermohaline circulation in those theories.

What determines the depth  $H$ ? Boccaletti et al. (2004) propose that a balanced heat budget for the ocean is the relevant constraint. In Fig. 1b the ocean is seen to gain a very large amount of heat in the equatorial upwelling zone. This would lead to a rapid deepening of the thermocline were it not for the currents that transport the warm water poleward so that the heat is lost in higher latitudes, especially where cold, dry continental air flows over the warm Kuroshio (and Gulf Stream in the Atlantic). In a state of equilibrium the gain must equal the loss. Should there be a warming of the atmosphere in midlatitudes that reduces the oceanic heat loss, then warm water accumulates in low latitudes so that the thermocline deepens. The winds then fail to bring cold water to the surface at the equator, the gain of heat is reduced, and a balanced heat budget is restored. This diabatic mechanism whereby surface conditions in higher latitudes can influence the depth of the thermocline in low latitudes on short time scales on the order of decades—those of the wind-driven circulation—is confirmed by scale analyses and numerical experiments with a general circulation model of the ocean (Boccaletti et al. 2004; Philander and Fedorov 2003). These calculations show that the key factors that determine the thermal structure of the ocean are the heat fluxes across the ocean surface, the winds that drive the ocean, and the diffusivity of the ocean. The latter parameter is of prime importance to the thermal structure at depth, which in turn influences the depth of penetration of the wind-driven circulation.

Both components of the oceanic circulation, the deep thermohaline and the shallow ventilated thermocline circulation, involve meridional overturning and both contribute to the poleward transport of heat by the oceans. A freshening of the surface waters in high latitudes can inhibit the sinking of cold water and hence can interfere

with the heat transports. This matter has been studied extensively in connection with the thermohaline circulation (which is sometimes referred to as conveyor belt), and it has been established that a sufficiently large freshening in high latitudes can lead to a shutdown of the thermohaline circulation (Manabe and Stouffer 1995, 2000; Rahmstorf 1995, 2000; Stocker and Schmittner 1997; Alley et al. 2003; Seidov and Haupt 2002, 2003). The impact of such a “shutdown” on the earth’s climate is prominent mainly over the northern Atlantic and western Europe. The reason for a shutdown can be inferred from the linearized expression for the equation of state that describes the dependence of density  $\rho$  on temperature  $T$  and salinity  $S$ :

$$\rho = \rho_0(1 - \alpha T + \beta S), \quad (1)$$

where  $\rho_0$ ,  $\alpha$ , and  $\beta$  are constants (in general,  $\alpha = \rho_0^{-1} \delta\rho/\delta T$  and  $\beta = \rho_0^{-1} \delta\rho/\delta S$  are functions of temperature and salinity). An oceanic circulation is possible in the absence of winds provided a density gradient  $\Delta\rho$  is imposed at the surface and there is sufficient mixing in the deep ocean (e.g., Wunsch 2002). The maintenance of warm conditions in low latitudes/cold conditions in polar regions drives such a circulation. If density should depend on temperature only, then this circulation disappears when the imposed meridional temperature gradient  $\Delta T$  vanishes. In the presence of salinity variations, the meridional density gradient, and hence the thermal circulation, can disappear even in the presence of a meridional temperature gradient. Equation (1) implies that this happens when

$$\Delta\rho = \rho_0(\alpha\Delta T - \beta\Delta S) \rightarrow 0 \text{ or } R \rightarrow 1, \quad (2)$$

where

$$R = \beta\Delta S/\alpha\Delta T.$$

In the case of the thermohaline circulation the limit  $R \rightarrow 1$  is known to be associated with a “breakdown” of that circulation (e.g., Zhang et al. 1999). Such singular behavior occurs because, for the thermohaline circulation, the equator-to-pole density difference  $\Delta\rho$  at the surface is also a measure of the vertical density gradient (or the vertical stability of the ocean) in low latitudes. [Note that the plus and minus signs in Eq. (2) are chosen for positive  $\Delta\rho$ ,  $\Delta T$ , and  $\Delta S$ .]

Salinity variations are acknowledged as being of paramount importance to the thermohaline circulation, but their effect on the circulation of the ventilated thermocline has thus far received scant attention. That salinity variations can nonetheless have a major influence on the ventilated thermocline is evident in Fig. 2, which shows how temperature and salinity vary on an isopycnal surface on which fluid parcels travel after subduction. In Fig. 2a, temperature variations are as large as  $10^\circ\text{C}$  on the  $1025 \text{ kg m}^{-3}$  density surface, which passes through the core of the Equatorial Undercurrent. Figure 2b shows that the warm water is saline and the cold water is relatively fresh, so that the density remains

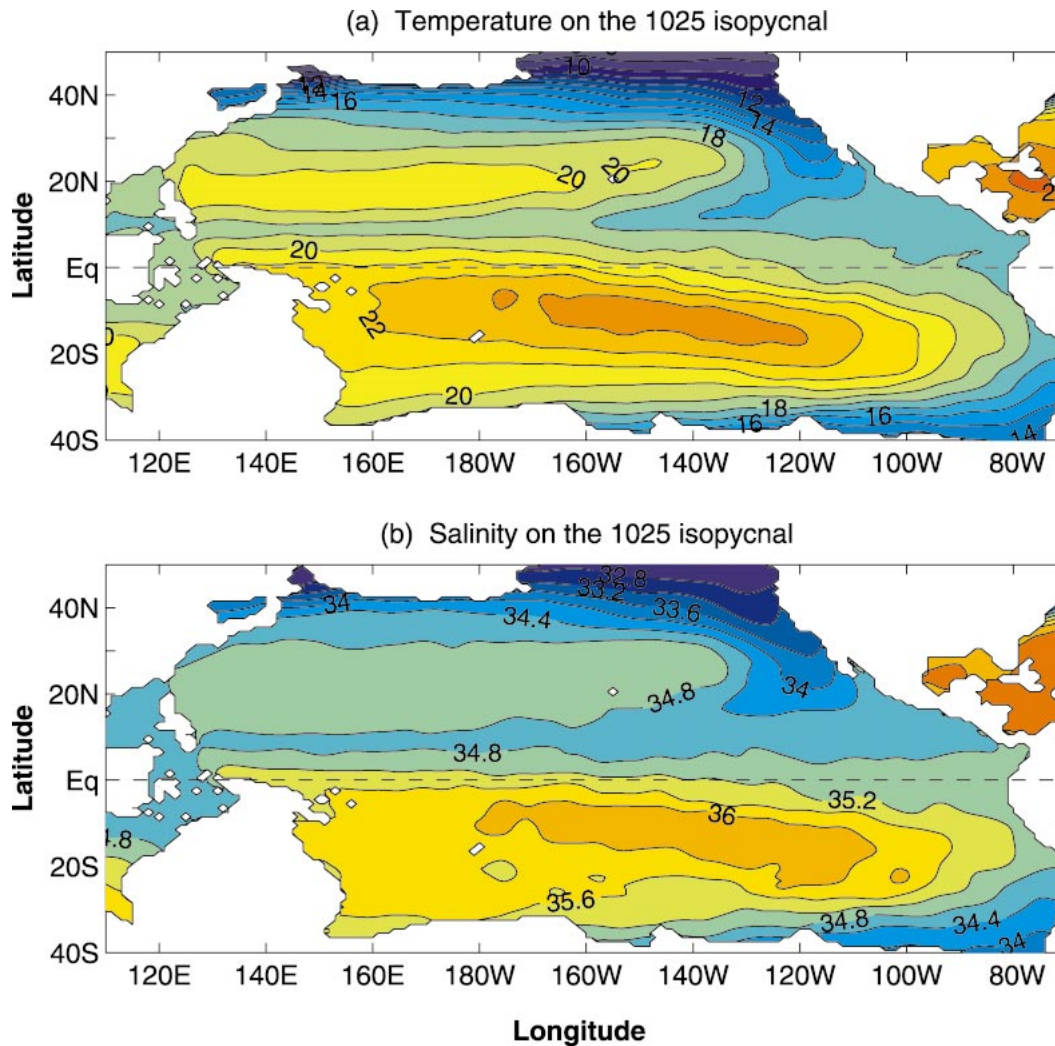


FIG. 2. (a) Temperature and (b) salinity variations on the 1025  $\text{kg m}^{-3}$  density surface in the Pacific Ocean, from the Levitus dataset (Levitus et al. 1994; Levitus and Boyer 1994).

constant. These variations of salinity on the isopycnal surface (on the order of 2–3 psu) reflect salinity variations at the surface where the waters are generally saline in low latitudes (except under the intertropical convergence zone) and are fresh in high latitudes.

How will a further freshening of the extratropical waters, especially those near the subduction zone, affect the oceanic circulation and its heat transport? This paper addresses this question in the spirit of Stommel's (1961) seminal study of the thermohaline circulation in a highly idealized situation. Our goal is, therefore, not a realistic simulation of detailed aspects of the climate but rather the elucidation of some of the processes that influence climate, specifically the processes that influence the way salinity variations can affect the wind-driven circulation of the upper ocean. To maintain a narrow focus, we introduce a number of idealizations that include the following: the winds that drive the oceanic circulation are regarded as given and the properties of the deep ocean,

which may change on much longer time scales, are also regarded as given. These idealizations preclude detailed comparisons between our results and observed climate phenomena because, in reality, the effects of changes in salinity on sea surface temperatures will alter the winds that drive the ocean. The first step toward understanding the resultant complex interactions between the ocean and atmosphere is an understanding of the simpler problem with which this paper is concerned. The results to be presented here are therefore but the first of a series that gradually will approach complex reality.

## 2. The models and methods

Studies of the deep thermohaline circulation have to take into account that it is relatively slow, with a time scale on the order of a millennium. Given limited computer resources, investigators choose a relatively coarse



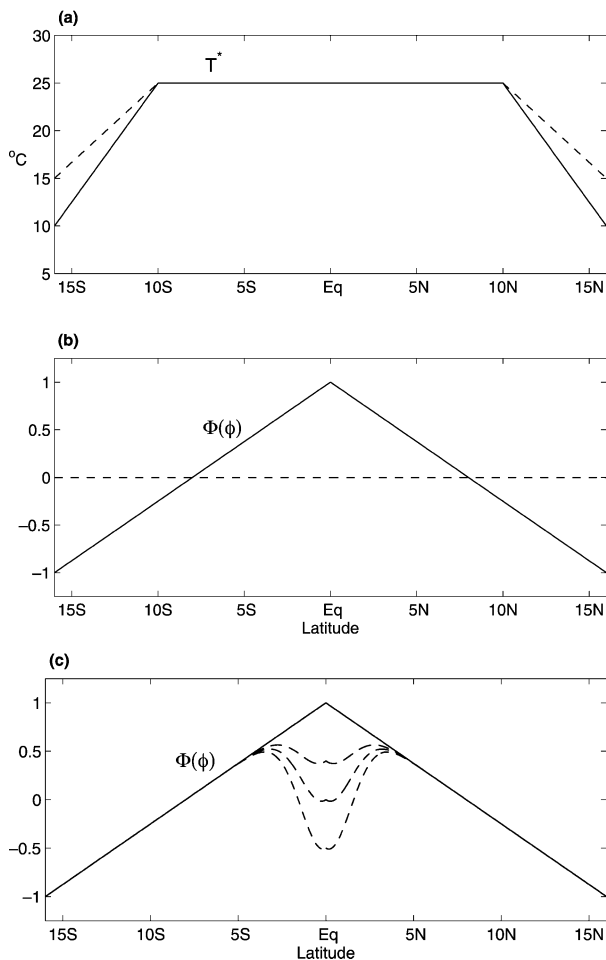


FIG. 3. (a) The meridional structure of the restoring temperature  $T^*$  (the solid line) used in the small-basin calculations. The dashed line shows the restoring temperature that was used to explore the sensitivity of the results to changes in the imposed meridional temperature gradient  $\Delta T$ . (b) The shape of the salinity forcing  $\Phi(\phi)$  used in most of the small-basin calculations. (c) The modified structure of the salinity forcing with a local minimum in the equatorial region that simulates the freshening of the ocean surface induced by rains in the ITCZ and over the western Pacific warm pool. The dashed lines in (c) correspond to different magnitudes of the equatorial freshening.

spatial resolution to compensate for the demands of simulations of equilibrium states. This paper focuses on the relatively rapid circulation of the ventilated thermocline—time scales are on the order of a decade—so that simulations of equilibrium states require relatively little computer resources. However, spatial resolution has to be high to cope with features such as a thin thermocline and narrow equatorial upwelling. To facilitate the study of a large number of cases we configured an idealized version of the oceanic general circulation model, known as MOM 4 (Griffies et al. 2001), to capture the feature of the wind-driven circulation that is most sensitive to variations in surface salinities, namely the meridional overturning involving subduction in higher latitudes and

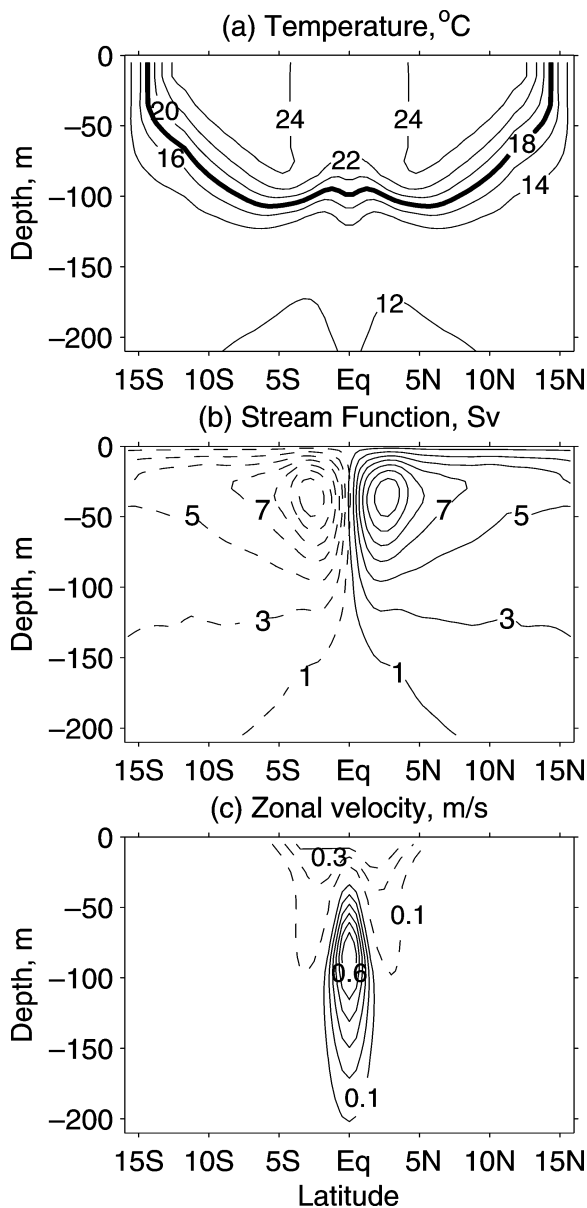


FIG. 4. A typical meridional section of the model solutions with no salinity forcing, i.e., in Eq. (5)  $B = 0$ : (a) the thermal structure at the middle of the basin, (b) the zonally integrated streamfunction (note the shallow overturning circulation connecting the Tropics and extratropics), and (c) the zonal velocity contours showing the Equatorial Undercurrent.

equatorial upwelling. To this end, the first series of experiments are with a model of modest dimensions—a rectangular basin  $40^{\circ}$  wide that extends from  $16^{\circ}\text{S}$  to  $16^{\circ}\text{N}$ —and with high resolution of  $0.5^{\circ}$  in the horizontal and 32 layers in the vertical direction to a depth of 5000 m. The winds that force the model are westward and are spatially uniform of intensity  $0.5 \text{ dyn cm}^{-2}$ .

The vertical diffusion of heat and momentum depends on a Richardson number (Pacanowski and Philander 1981) and has the background vertical diffusion  $k =$

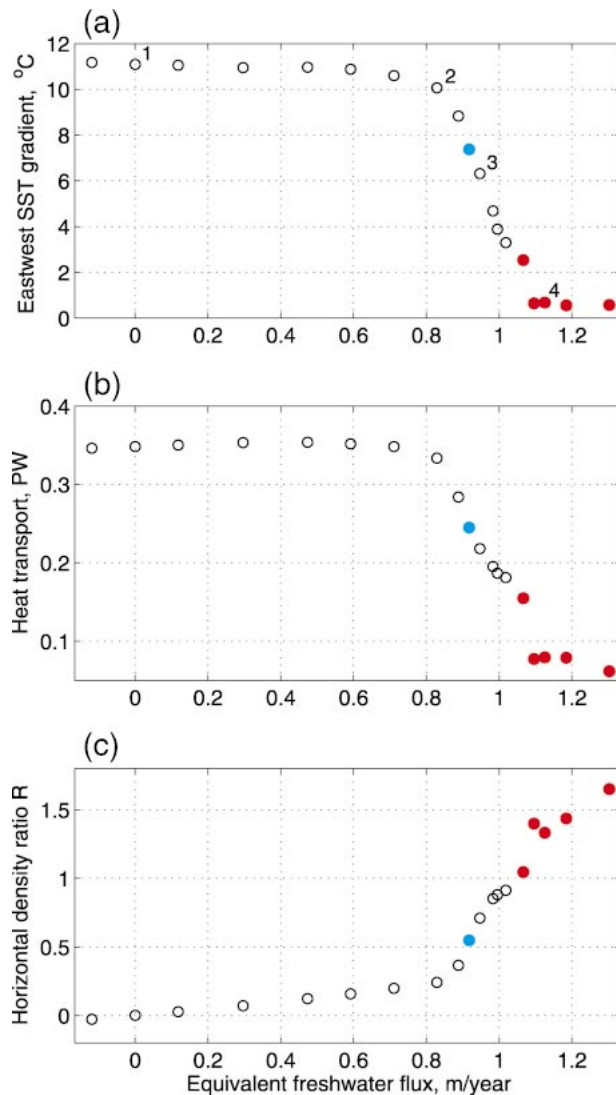


FIG. 5. Changes in (a) the equatorial east–west surface temperature gradient, (b) the meridional heat transport across a fixed latitude ( $8^{\circ}\text{N}$ ), and (c) the density ratio  $R$  as the flux of freshwater onto the surface near the northern boundary of the basin increases. The value of  $R$  today, indicated by a blue dot, is such that current conditions are sensitive to relatively modest changes in the warming or freshening of surface waters in higher latitudes. The red dots correspond to cases with  $R > 1$ . Numbers 1, 2, 3, and 4 indicate cases shown in Figs. 7–11. The values of the freshwater flux are calculated by averaging  $(e - p)$  over the region where it is positive and rescaling it to a realistic-size basin (using a factor of 3).

$0.01 \text{ cm}^2 \text{ s}^{-1}$ . The maximum vertical diffusion reaches  $50 \text{ cm}^2 \text{ s}^{-1}$  in the areas of the strong vertical shear associated with the Equatorial Undercurrent. The horizontal diffusion  $k_h$  is  $2 \times 10^7 \text{ cm}^2 \text{ s}^{-1}$  in the momentum equations and  $1 \times 10^7 \text{ cm}^2 \text{ s}^{-1}$  in the salinity and heat equations. A linear Rayleigh damping is added at the southern and northern walls, but only in the momentum equations, which was sufficient to filter out or weaken boundary Kelvin waves. No additional Rayleigh damping was used in the salinity and temperature equations, since

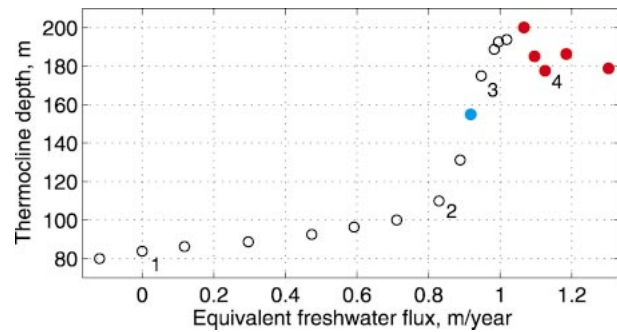


FIG. 6. Changes in the mean depth of the equatorial thermocline as the flux of freshwater increases. The blue dot indicates current conditions. The red dots correspond to cases with  $R > 1$ . The depth of the thermocline is estimated in the middle of the basin (at  $0^{\circ}$ ,  $20^{\circ}\text{W}$ ) by calculating the depth at which the vertical derivative of temperature,  $dT/dz$ , is maximum.

it would interfere with the surface heat and freshwater fluxes. In several sensitivity experiments, instead of using vertical and horizontal diffusivities, we applied an isoneutral mixing scheme, but the results were essentially unaffected.

We use standard mixed boundary conditions on the salt and temperature (e.g., Zhang et al. 1999):

$$kT_z = A(T^* - T) \quad \text{and} \quad (3)$$

$$kS_z = (e - p)S_o, \quad (4)$$

where  $A \approx 1 \text{ m day}^{-1}$  is a constant (equivalent to  $50 \text{ W m}^{-2} \text{ }^{\circ}\text{C}^{-1}$  in terms of the heat flux),  $z$  is the vertical coordinate,  $(e - p)$  is evaporation minus precipitation and river runoff,  $S_o$  is the mean salinity in the basin,  $T$  is the sea surface temperature, and  $T^*$  is an imposed temperature. A difference between  $T$  and  $T^*$  implies that the heat flux in and out of the ocean is nonzero. As long as the ocean dynamics can change this difference, the heat transport will be important.

The term  $(e - p)$  is parameterized as

$$e - p = B\Phi(\phi) - \Phi_o, \quad (5)$$

where  $B$  is a constant,  $\Phi(\phi)$  is the latitudinal structure of the forcing ( $\phi$  is latitude), and  $\Phi_o$  is a correction such that the overall mean of the forcing is zero. There is no salt or heat flux through the basin walls. The surface boundary condition is a restoring one for temperature (Haney 1971) but for salinity [Eq. (4)] it is a virtual salt flux through the ocean surface [similar boundary conditions are used in Zhang et al. (1999), for instance]. The use of mixed boundary conditions is related to simple physical arguments: the heat flux depends on evaporation that in turn depends on surface temperatures, but the freshwater flux, to a first approximation, does not depend on the local salinity. The oceanic response can modify the extent to which it is forced thermally, but that is not so in the case of salt. Does this imply that the salinity forcing can reach critical levels that induce marked changes in the response? This is known

to be the case in the thermohaline circulation. Is there a similar phenomenon for the wind-driven circulation of the ventilated thermocline?

The latitudinal structure of the forcing is shown in Figs. 3a and 3b, with  $T^* = 25^\circ\text{C}$  near the equator, decreasing to  $10^\circ\text{C}$  at the northern and southern walls, and  $\Phi(\phi)$  equal to 1 at the equator, decreasing linearly to  $-1$  at the walls;  $\Phi_o$  is small, but nonzero, because of sphericity of the basin. The value of  $B$  changes from one experiment to the next (dashed lines in Fig. 3b);  $B = 0$  means that there are no salinity variations. This form of the salt flux allows us to simulate the freshening of surface waters in high latitudes without changing the mean salinity of the ocean. Several sensitivity experiments were completed in which we used an explicit freshwater-flux boundary condition instead of the virtual salt flux and prescribed the water flux in the free-surface boundary condition. No major differences were found. A number of experiments were completed with  $T^*$  decreasing to  $15^\circ\text{C}$  near the walls (the dashed line in Fig. 3a), rather than  $10^\circ\text{C}$ . In other experiments the shape of  $\Phi(\phi)$  was modified to include a “dip” in the salinity forcing (Fig. 3c) in order to investigate the effect of local freshening of the ocean surface in the ITCZ and over the western Pacific warm pool.

At the beginning of a set of calculations the ocean is at rest, isothermal, and isohaline. After the sudden onset of uniform easterly winds, calculations continue for 30 years in the case of the small ocean basin. By that time the initial adjustment is completed, and the circulation of the ventilated thermocline is in a state of quasi equilibrium. The deep ocean is still in a state of very gradual adjustment, but this is of secondary importance to the phenomena being investigated here because the oceanic heat budget is close to being balanced with the heat loss in high latitudes nearly equal to the heat gain in low latitudes. The small discrepancy from a balanced heat budget disappears gradually as the deep thermohaline circulation comes into equilibrium. (This strategy of simulations for a relatively short period, a few decades, exploits the considerable difference in the time scales associated with these two circulations—a decade and a millennium respectively.) In a few additional experiments, described in section 4, the calculations are continued for several centuries to examine possible long-term trends.

The model described above is unrealistic in several respects: the meridional extent of the basin is very modest, the regions of subduction are along the northern and southern walls, and intense western boundary currents (Kuroshio or Gulf Stream) are absent because the winds have no curl (a weak frictional western boundary current is still present in the model). We therefore conducted a second set of experiments, described in section 5, for an ocean basin with a much larger latitudinal and longitudinal extent—close to that of the Pacific Ocean—and with winds with a curl so that the subtropical gyre has an intense western boundary current. The more re-

alistic winds and ocean size do not alter the main results significantly, thus justifying the use of the smaller basin, which requires much less computer resources and is more convenient for conceptual purposes. That the unrealistic features of the first set of experiments are of secondary importance could have been anticipated. For example, the presence of a western boundary current is not necessary for meridional overturning. Furthermore, whether wind-induced subduction occurs along a wall or where westerly and easterly winds induce Ekman layer convergence is not of critical importance. Last, the most important internal latitudinal scale is the radius of deformation—the width of the region of equatorial upwelling, for example—which is far smaller than  $16^\circ$  latitude, the latitudinal extent of the small basin.

### 3. The results for a small ocean basin

In our reference case the ocean is initially at rest and is isothermal and isohaline, with a temperature of  $10^\circ\text{C}$  and salinity of 35 psu. After the sudden onset of uniform easterly winds and the thermal forcing of Eq. (3)—no salinity forcing is applied so that  $B = 0$  in Eq. (5)—calculations continue for 30 years by which time the circulation of the ventilated thermocline is essentially in a state of equilibrium. The meridional thermocline structure of the flow is shown in Fig. 4. The model, despite its modest dimensions and simple setting, gives a reasonable representation of the thermocline ventilation and the shallow overturning cell with water parcels sinking along the poleward walls, traveling along isopycnals towards the equator, joining the Equatorial Undercurrent (see Fig. 4c), and rising to the surface as part of the equatorial upwelling. Subsequently the flow is poleward in surface Ekman layers (Fig. 4b). The slope of the thermocline along the equator and the sea surface temperature variations will be shown in the top panels of Fig. 7. Boccaletti et al. (2004) describe the effect of changes in  $T^*$  (and  $\Delta T$ ) on this motion when no salinity variations are present. Here we explore the effect of introducing salinity variations.

In the next set of experiments we perturb the ocean conditions by introducing a source of freshwater at the surface near the northern and southern boundaries. To do that, we fix  $T^*$  and vary freshwater and salinity fluxes by increasing  $B$  (see Fig. 3b)—such a procedure increases both the freshwater supply at high latitudes and the salt flux at low latitudes so that the mean ocean salinity does not change.

The linearized equation of state [Eq. (1)] gives the impression that a decrease in temperature and an increase in salinity affect oceanic conditions similarly. It is already known from the study of Boccaletti et al. (2004), who neglect salinity variations, that a decrease in the meridional temperature gradient  $\Delta T$  at the surface causes a decrease in the poleward heat transport. The inclusion of salinity variations alters this result, not only quantitatively as the equation of state would suggest but

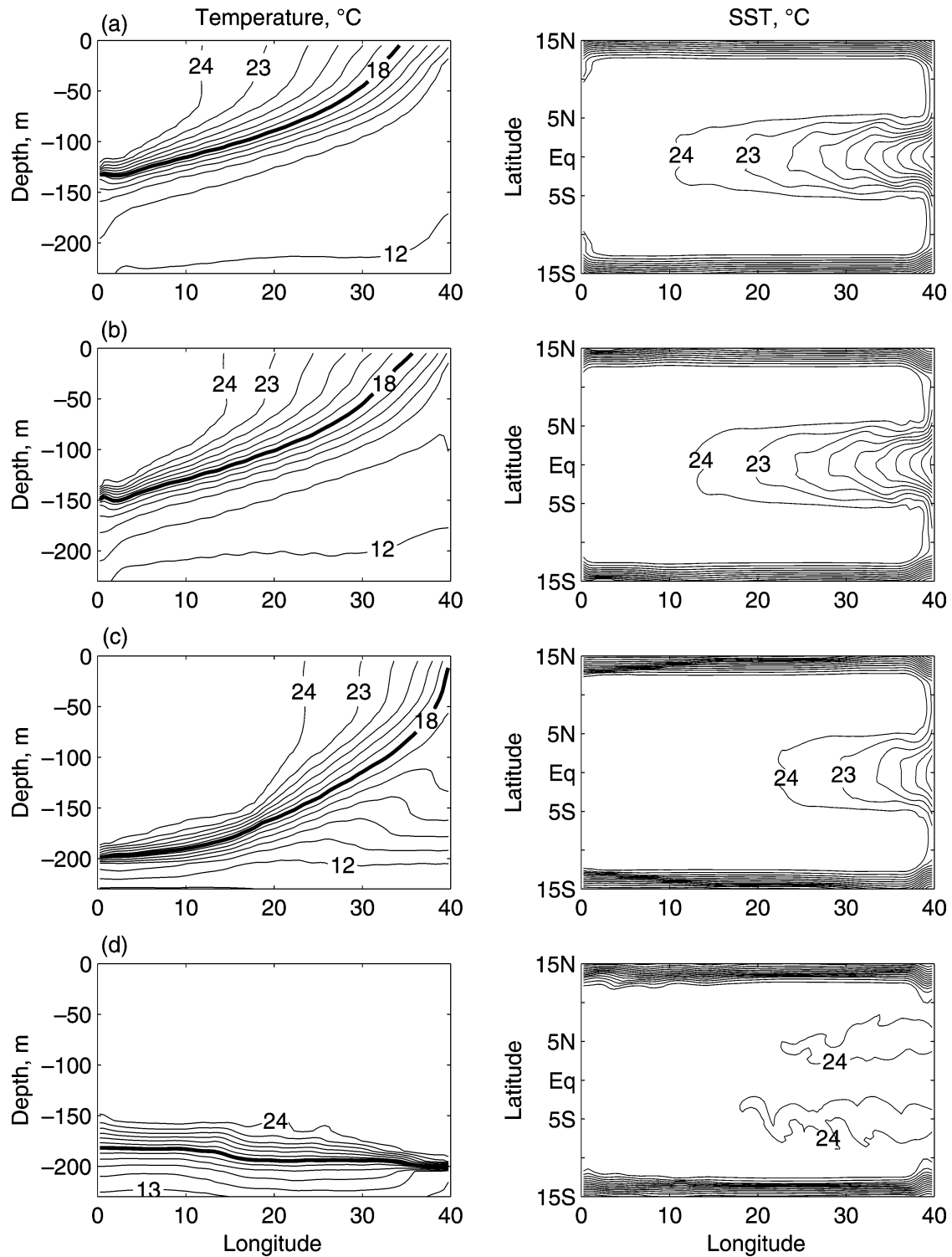


FIG. 7. (left) The thermal structure of numerical solutions in the equatorial plane and (right) the corresponding sea surface temperatures for the small-basin calculations. Notice the collapse of the thermocline in the bottom panels. The freshwater forcing increases from top to bottom. Cases 1, 2, 3, and 4 as indicated in Figs. 5 and 6 are shown; the freshwater forcing increases from top to bottom [in Eq. (5),  $B = 0, 1.6, 1.8, 2.1 (\times 10^{-7} \text{ m s}^{-1})$ ].



also qualitatively, in particular because of the different boundary conditions for temperature and salinity in Eqs. (3) and (4). The results show that, when the freshwater forcing reaches a certain amplitude, the decrease in heat transport suddenly approaches a threshold. This is evident in Figs. 5 and 6, which depict how changes in freshwater forcing affect the surface temperature gradient along the equator, the poleward heat transport, the simulated density ratio  $R$  [and hence the value of meridional salinity gradient  $\Delta S$ ; see Eq. (2)], and the depth of the equatorial thermocline. As the freshwater flux near the poleward walls increases from one experiment to the next, the different parameters are seen to change slowly at first and then rapidly as the flux approaches a critical value (and  $R$  approaches 1).

The slope of the thermocline along the equator and the sea surface temperature variations for four different values of the freshwater forcing (indicated as 1, 2, 3, and 4 in Fig. 5) are displayed in Fig. 7. The top row of panels of this figure shows the thermocline slope and SST of the reference solution (case 1) with no salinity variations imposed. The second row of panels shows the thermal structure for a relatively weak salinity forcing—the solution is still dominated by temperature and salinity variations have little effect on either thermocline or SST. A further freshening of the surface waters near the northern and southern boundaries, and the associated reduction in the meridional density gradient at the surface, deepens the equatorial thermocline (also Fig. 6) and reduces both the size of the equatorial cold tongue and the oceanic heat gain in low latitudes (the third and fourth rows in Fig. 7). The corresponding changes in spatial structures in salinity (in the equatorial plane and at the surface) and density (along a meridian and in the equatorial plane) are shown in Figs. 8 and 9, respectively.

When  $R > 1$  (the red dots in Figs. 5 and 6 and the bottom panels in Fig. 7), the thermocline slope in the equatorial plane collapses, the cold equatorial tongue at the surface virtually disappears, and permanently warm (El Niño-like) conditions<sup>1</sup> prevail in the Tropics. The collapse of the thermocline eliminates the confined equatorial region where the ocean gains a large amount of heat. As a result, the constraint of a balanced heat budget is no longer satisfied by transporting heat from regions of gain to regions of loss. Rather, the heat budget tends to be balanced more locally (Fig. 10) and the heat transport from the equatorial region is significantly reduced. (A local balance can be simulated by means of a one-dimensional mixed layer model that takes into account only vertical variations in density. Such a balance implies that there is little difference between  $T$  and  $T^*$ .) Apparently such a state of affairs can be induced merely by freshening the surface waters in the extra-

<sup>1</sup> Referring to this state as permanently warm conditions or permanent El Niño, we imply the absence of a zonal SST gradient along the equator.

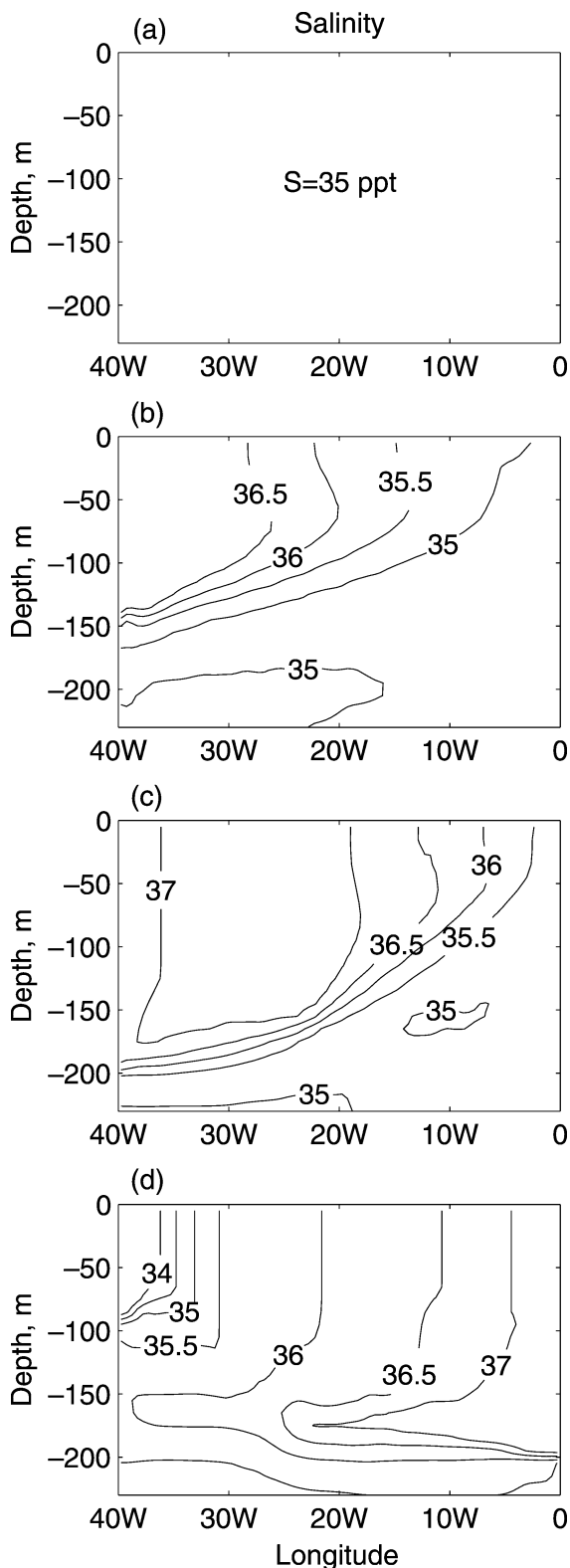


FIG. 8. The salinity structure of the numerical solutions in the equatorial panel. There are no salinity variations in the upper panels. Note the west-to-east redistribution of salt after the thermocline collapse. From top to bottom: cases 1, 2, 3, and 4.

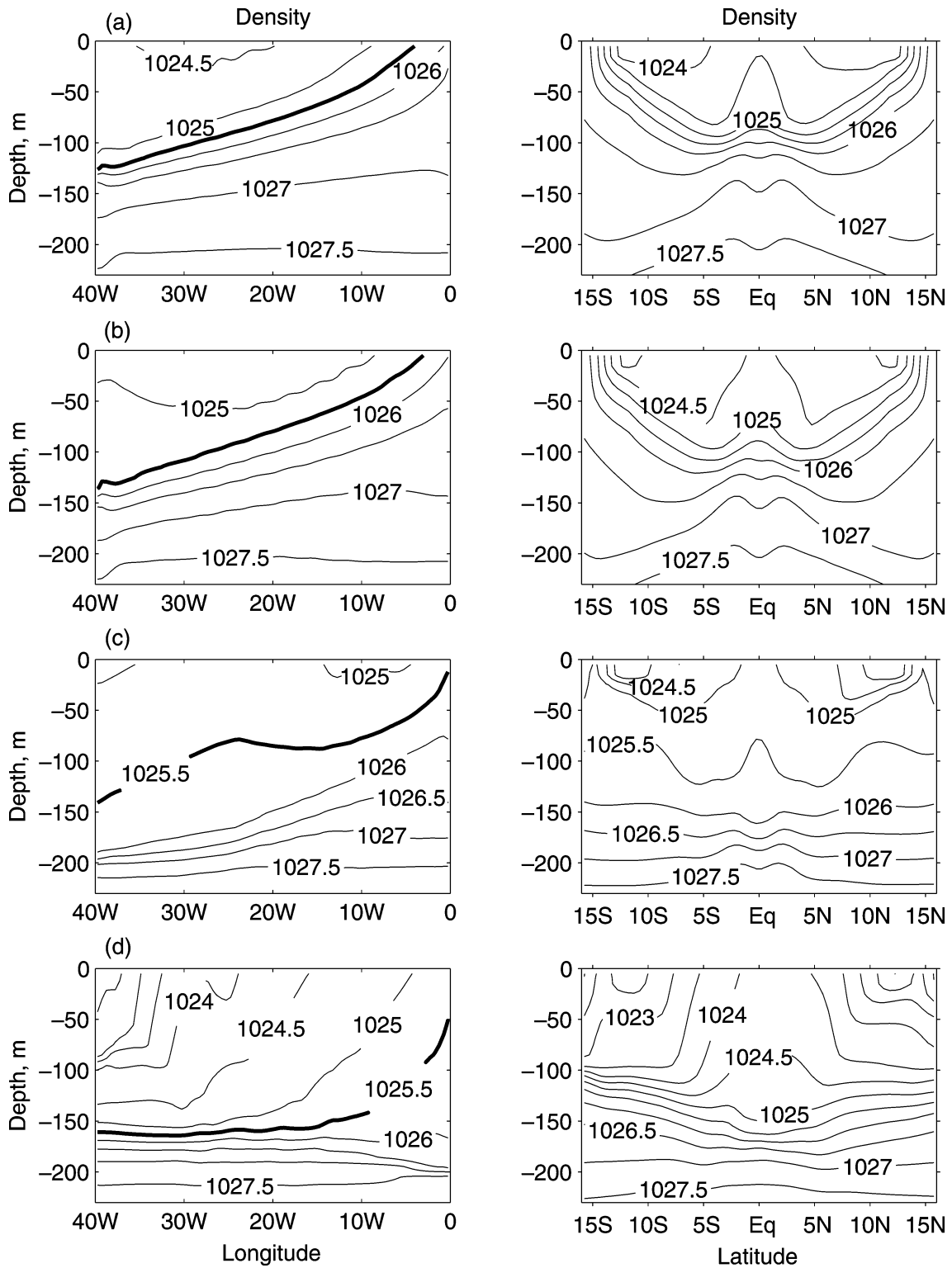


FIG. 9. The density structure of the numerical solutions in the (left) equatorial plane and (right) along a middle meridian. From top to bottom: cases 1, 2, 3, and 4.

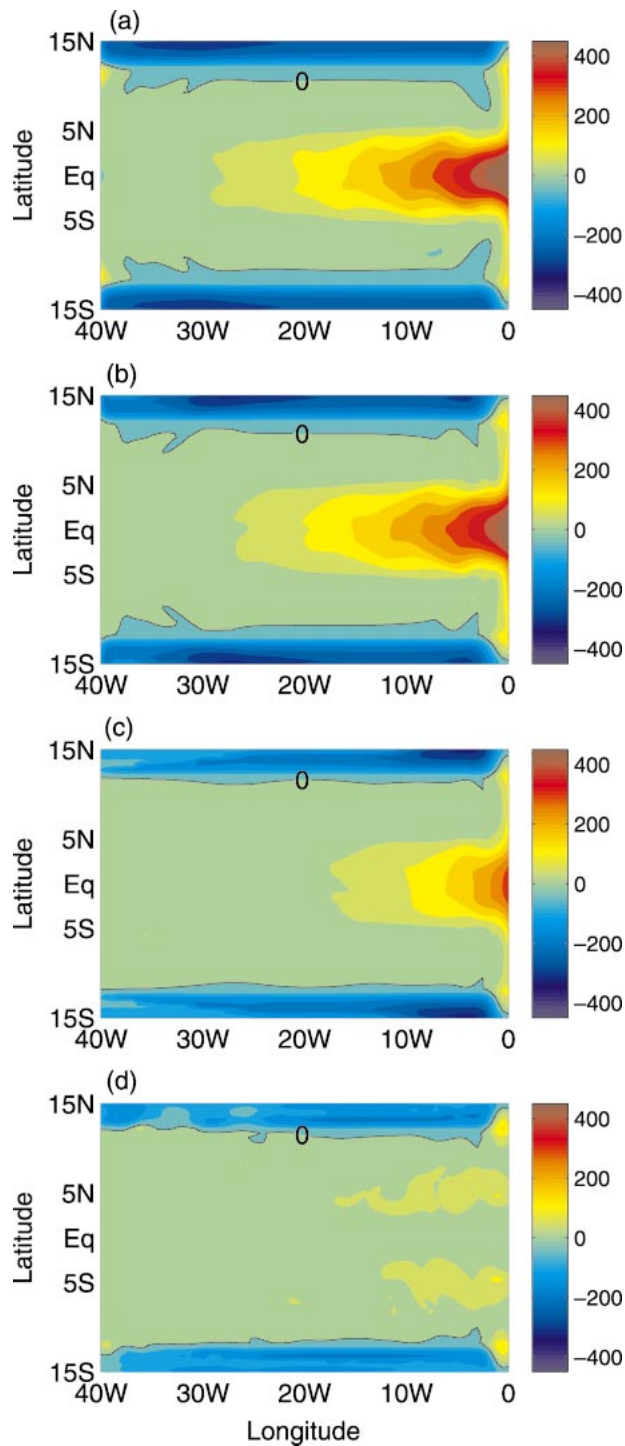


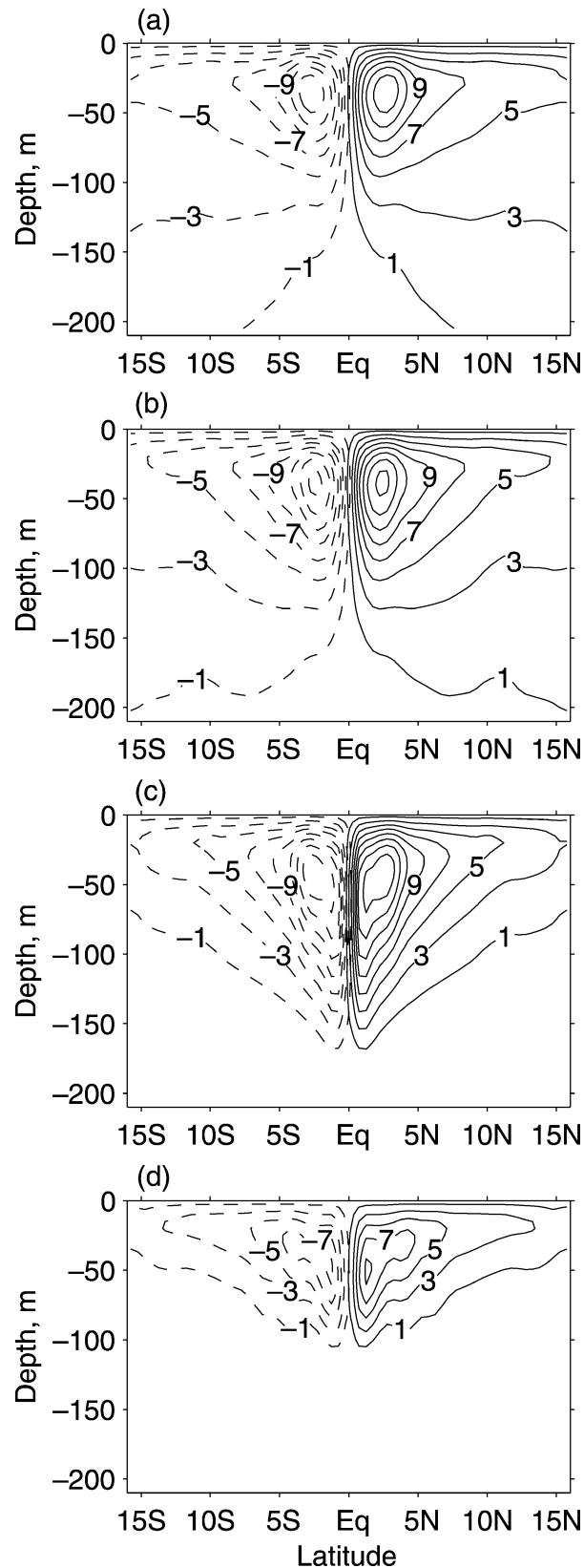
FIG. 10. (a)–(d) The downward heat flux ( $\text{W m}^{-2}$ ) for the solutions shown in the previous figures. The net heat flux into the ocean is zero in (a)–(d). A small positive constant corresponding to a gradual diffusion of heat into the deep ocean was subtracted from the data. In (a) and (b) the heat loss near the poleward walls is balanced mainly by the heat gain in the equatorial cold tongue, while in (c) and (d) the heat budget is more local. Note that even in (d) the heat fluxes in and out of the ocean never vanish completely, which implies a residual poleward heat transport.

tropics. In these experiments the winds have remained unchanged so that a zonal pressure gradient along the equator is still needed to balance the winds. With the collapse of the thermocline, that density gradient depends mainly on salinity. The surface water of the eastern Pacific, instead of being cold, is saline, as shown in the bottom panels of Fig. 8.

Given how abruptly the equatorial thermocline can collapse in Fig. 5, it is important to estimate how far oceanic conditions today are from singular behavior near  $R = 1$ . Our results, for a small idealized model of the ocean, need to be rescaled to be appropriate for the much larger Pacific. This difficulty can be sidestepped by focusing on the nondimensional parameter  $R$ . Its value today, approximately 0.5 (see the appendix), is indicated by a blue dot in Figs. 5 and 6. The results imply that climatic conditions today—high latitudes with heavy rains and river runoff that freshen the surface waters and hence counter the effect of the decrease in temperature with increasing latitude—may put us in a parameter range of relatively high sensitivity to changes in surface buoyancy. Relatively modest changes in the freshening of surface waters (because of the melting of ice or intensification of the global hydrological cycle) may result in a transition to permanent El Niño conditions. Because of the nonlinearity of the equation of state of water and complicated geometry of the ocean,  $R = 0.5$  is given here as only a very rough estimate. In fact, any value of  $R$  between 0.3 and 1 would put the conditions of today on the steep slope in Figs. 5 and 6.

The equatorial thermocline collapses when the flux of freshwater onto the surface in extratropical regions is such that the meridional density gradient at the surface vanishes. The cold, fresh surface water near the northern and southern walls then has such a low density that the wind-driven warm, saline water drifting poleward in the Ekman layer subducts beneath the surface water before reaching the northern and southern walls. This can be seen, for instance, from the plots of the meridional streamfunction (Fig. 11). The subduction of surface water relatively far from the northern or southern wall, and a weaker transport of water through high latitudes, decreases the loss of heat to the atmosphere, causing a reduction in the heat gained near the equator by means of a deepening of the equatorial thermocline. Salinity gradients along the equator now balance the wind stress. The thermal structure presumably continues to change because of diffusive processes with a long time scale. To investigate such changes we continued some of the simulations for several centuries (see section 4).

We also investigated the sensitivity of the results to the values of the restoring coefficient  $A$  (inversely proportional to the relaxation time scale), which is critical in controlling how far away  $T$  can drift from  $T^*$ . Although qualitatively the results did not change, one important tendency is worth mentioning. When the relaxation time increases and the connection between  $T$  and  $T^*$  weakens, it becomes much easier for the thermocline



collapse to take place. In other words, for smaller values of  $A$  the collapse (seen in Fig. 5) would have occurred for a weaker freshwater forcing.

In other experiments the shape of  $\Phi(\phi)$  was modified to include an equatorial “dip,” or a local minimum in the salinity forcing (Fig. 3c) simulating the effect of local freshening of the ocean surface over the ITCZ and western Pacific warm pool. This modification of the forcing did not change our results qualitatively unless the local equatorial freshening was sufficiently strong to overpower the extratropical freshening. What mattered most was the strength of the imposed meridional salinity gradient  $\Delta S$  (from the equator to the northern/southern boundaries). As long as that gradient was sufficient to balance  $\Delta T$  (in terms of its effect on density), the thermocline collapse did happen.

Another set of numerical experiments was conducted to investigate the effect of changing meridional temperature gradient  $\Delta T$ . Boccaletti et al. (2004) investigated this problem in the absence of salinity and showed that a gradual reduction of  $\Delta T$  leads to a gradual deepening of the equatorial thermocline. Adding salinity introduces a new phenomenon—the possibility of a rapid thermocline collapse that can be induced solely by changing  $\Delta T$ . This is because the condition of thermocline collapse  $R = 1$  [Eq. (2)] can be satisfied either by increasing  $\Delta S$  (as in Figs. 5–6), or by decreasing  $\Delta T$ , provided that  $\Delta S$  is nonzero. Our numerical results do indeed show that it is possible to force such thermocline collapse by changing  $\Delta T$  (when  $\Delta S$  is fixed).

#### 4. Long-term trends

The results shown thus far are for calculations that continue for a few decades at most. In a few cases the calculations were continued for 500 years. For zero or weak freshwater forcing the results remained essentially unchanged. For the cases with relatively strong freshwater forcing the lenses of cold, fresh surface water near the northern and southern walls persist (Fig. 12) while the deep ocean continues to warm very gradually. The processes involved will apparently take far longer than 500 years to reach equilibrium. The ultimate stratification of the deep ocean is a matter beyond the scope of this paper and will be investigated on another occasion.

On a time scale of a few centuries, another intriguing phenomenon became apparent, one associated with a bifurcation of possible states (for the cases with no thermocline collapse). Although the equations being solved and the initial and the boundary conditions are all sym-

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FIG. 11. The zonally integrated streamfunction for the solutions shown in the previous figures. Note changes in the shallow overturning circulation connecting the Tropics and extratropics. Only the near-surface part of the overturning is important for the heat transport.



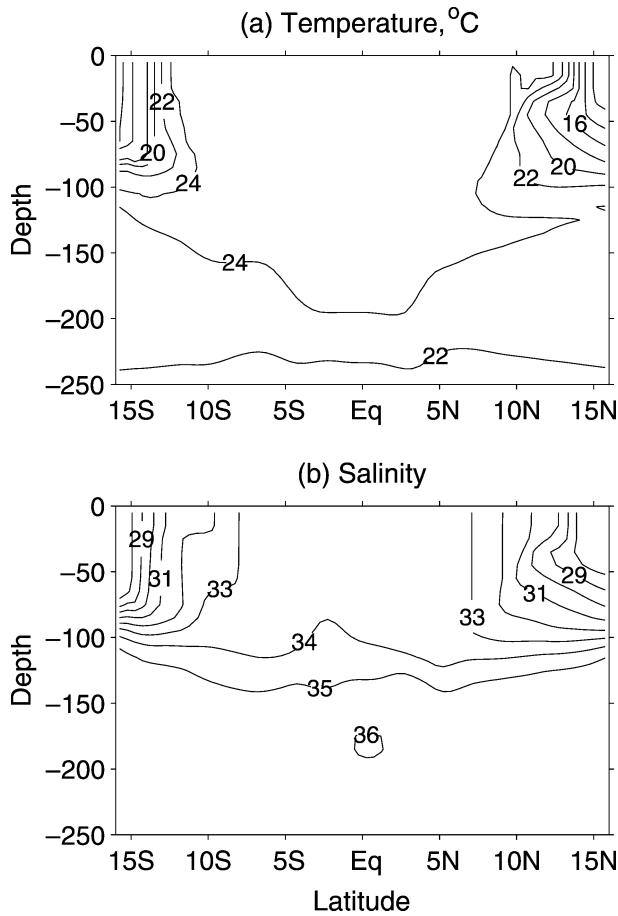


FIG. 12. The details of the meridional structure of numerical solutions after 500 years of integration (for case 4 of Figs. 5–9) for the small-basin calculations. The equatorial pycnocline is controlled mostly by salinity variations.

metrical about the equator, on several occasions the flow over the course of a few centuries acquired asymmetries relative to the equator. This is evident, for example, in Fig. 13, which corresponds to case 3 after 500 years. The thermal and salinity structure shows that water in the Southern Hemisphere is warmer and saltier than that in the Northern Hemisphere. A sharp boundary between relatively fresh and relatively salty waters appears along the equator. A tongue of cold and fresh water emanates from the subduction region in the north. These asymmetries relative to the equator are in response to extremely small asymmetries introduced by the numerical code. (Presumably, slightly different numerical noise can favor asymmetry that is the mirror image of the one in Fig. 13.) This means that the mean state seen in Fig. 4, when perturbed slightly, can drift into different possible states. A similar phenomenon—both symmetric and asymmetric equilibrium states—has been long known to be possible for the thermohaline circulation (e.g., Huang et al. 1992; Marotzke and Willeward 1991), but here we have shown that a weak bifurcation may also occur for the wind-driven circulation. Significantly,

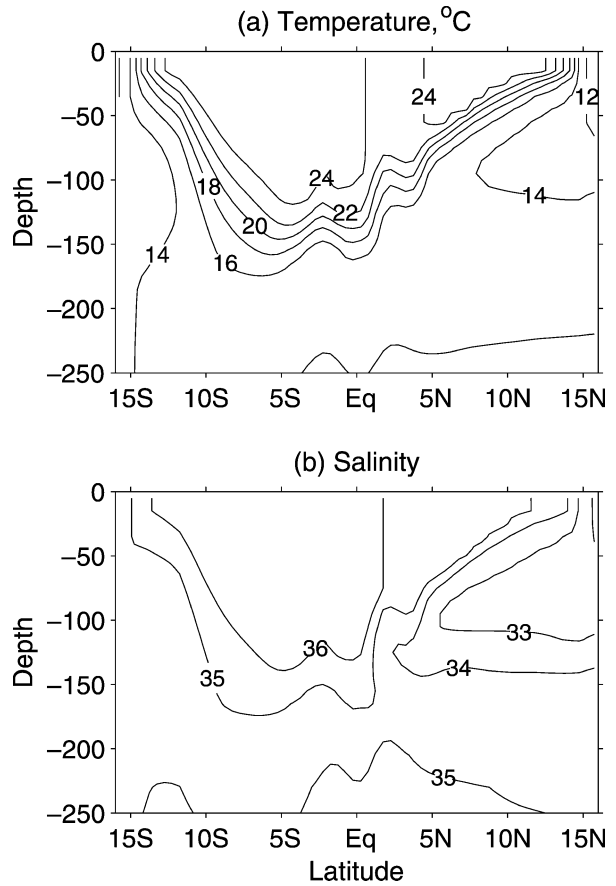


FIG. 13. The details of meridional structure of the numerical solutions after 500 years of integration (for case 3 of Figs. 5–9) for the small-basin calculations. A north–south asymmetry in the thermal and salinity structure has developed. The structure of the solution along the equatorial plane changed only slightly as compared with that shown in the third left-side panel of Fig. 7.

this effect was observed only in the vicinity of  $R = 1$  (case 2 did not reveal this type of bifurcation).

The thermal and salinity structures in Fig. 13 strongly resemble the actual distribution of temperature and salinity in the Pacific Ocean (Fig. 14). This observed asymmetry is strongly influenced by the asymmetrical surface forcing: it rains more in the Northern than Southern Hemisphere because the intertropical convergence zone is mostly north of the equator. The results in Fig. 13 suggest another factor that could contribute to the observed asymmetry, namely, the tendency of a symmetric mean state to drift to an asymmetric state as in Fig. 13.

### 5. The results for a large basin

The numerical experiments described thus far are for an ocean basin of modest dimensions, forced with winds without any curl. We next increase both the latitudinal and longitudinal extent of the basin, to 48°N–48°S and 120°E–80°W, respectively, which is close to the actual

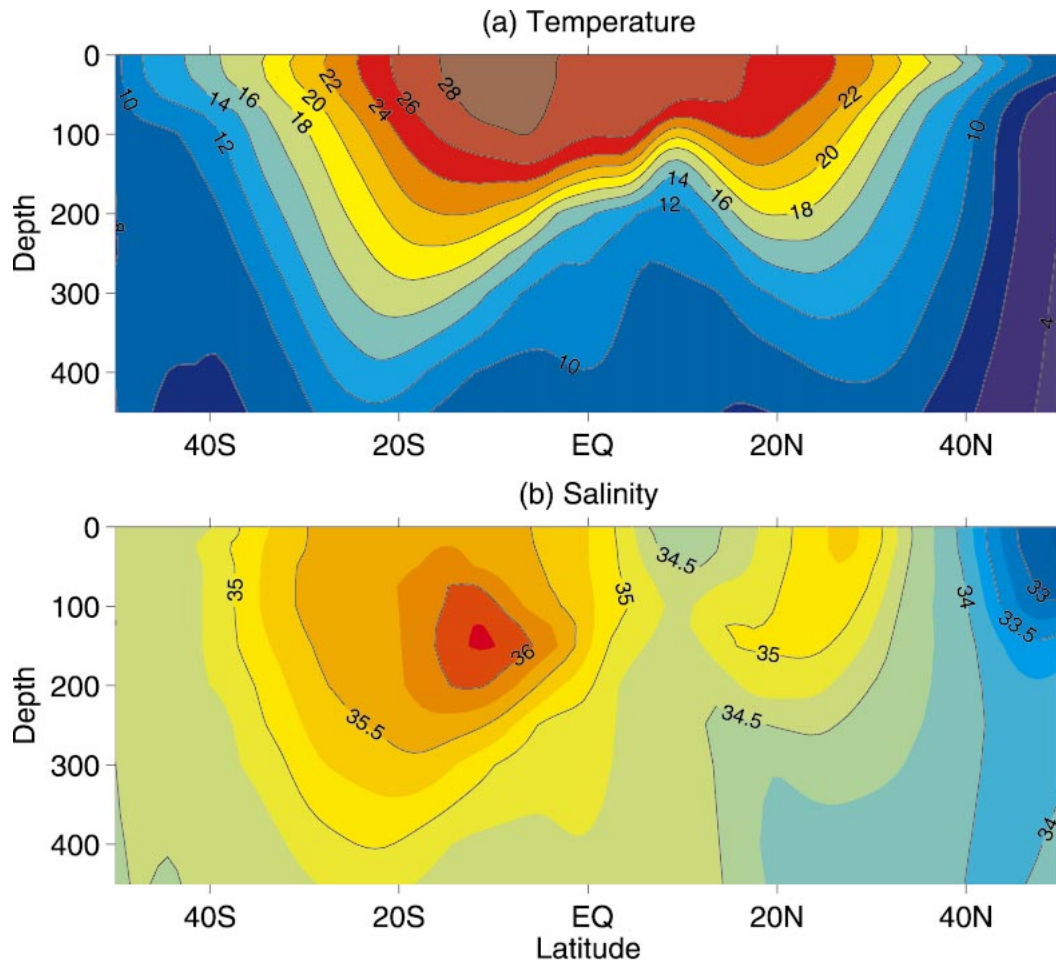


FIG. 14. Meridional (a) temperature and (b) salinity variations along 165°W in the Pacific Ocean (cf. Fig. 13).

size of the Pacific Ocean excluding the region of the subpolar gyre and regions adjacent to the Antarctic Circumpolar Current (ACC), and impose winds that generate a strong western boundary current. [We use an analytic approximation to the zonally averaged annual mean winds by Hellerman and Rosenstein (1983).] The imposed temperature  $T^*$  and the latitudinal structure of the salinity/freshwater forcing  $\Phi(\phi)$  are shown in Fig. 15. Calculations continue for 60 years. Because of these changes, the regions where the ocean loses heat and where surface water subducts no longer coincide.

The vertically integrated streamfunction (i.e., the Sverdrup flow) is plotted in Fig. 16a, which displays the characteristic subtropical gyres with frictional western boundary currents. The zonally integrated structure of the flow (i.e., the shallow meridional overturning) is given in Fig. 16b, which shows the strong subtropical cells associated with the thermocline ventilation. It is the similarity of the tropical circulation in Fig. 16b and Fig. 4b that justifies our use of a small basin in the previous sections.

As in the cases described for a small basin, the ther-

mocline still deepens and the size of the equatorial cold tongue still shrinks as the flux of freshwater onto the surface in high latitudes increases. This is evident in Fig. 17, which also shows, in the bottom panel, that for a sufficiently strong freshwater forcing the thermocline collapses. These aspects persist even though, in Fig. 18, a map of fluxes across the ocean surface, the strongest heat loss is seen to occur in the region where the western boundary current crosses the isotherms; the maximum heat gain is still in the region of the equatorial cold tongue. When the thermocline collapses and the cold tongue virtually disappears, the heat transport from the equatorial region is significantly reduced. A much broader area of heat gain is now needed to compensate for the heat loss in high latitudes.

An important difference between the heat fluxes for the small and large basins is that in the latter case the region of heat loss and the region of subduction are separated. A balanced heat budget is then achieved, as shown in Boccaletti et al. (2004), by means of a combination of advection, wave action, and diabatic effects over a time scale on the order of a decade. Significantly,

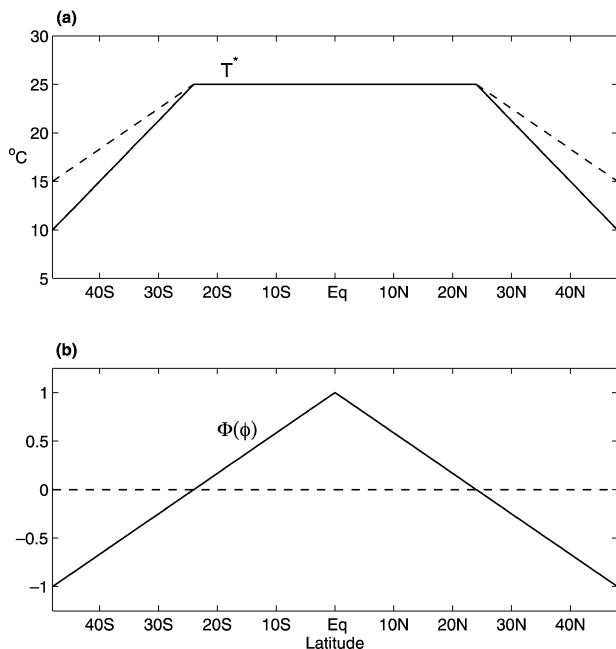


FIG. 15. (a) The meridional structure of the restoring temperature  $T^*$  (the solid line) used in the large-basin calculations. The dashed line shows the restoring temperature that was used to explore the sensitivity of the results to changes in the imposed meridional temperature gradient  $\Delta T$ . (b) The shape of the salinity forcing  $\Phi(\phi)$  used in the large-basin calculations.

no direct route from the subduction to heat-loss regions is necessary for balancing the heat budget.

**6. Conclusions**

The results described in this paper concern the effects of extratropical fluxes of freshwater onto the ocean surface on the shallow wind-driven circulation of the ventilated thermocline. In particular, we show that these effects have certain similarities with the impact of freshwater fluxes on the deep thermohaline circulation. A decrease in the meridional density gradient at the surface reduces the poleward heat transport of the circulation in both cases, sharply so when the density gradient approaches zero. Both cases allow the possibility of a bifurcation of the circulation, from a state of symmetry (with respect to the equator) to an asymmetric state, when the freshwater forcing in high latitudes is large enough. The changes in climate because of a sharply reduced poleward heat transport are strikingly different in the two cases. A much weaker thermohaline circulation affects climate conditions primarily in the northern Atlantic; a wind-driven circulation that fails to transport heat poleward is associated with a tendency toward a deep thermocline all along the equator, and permanent El Niño conditions. Since the processes involving the circulation of the ventilated thermocline can occur relatively fast, on the order of a few decades, the transition

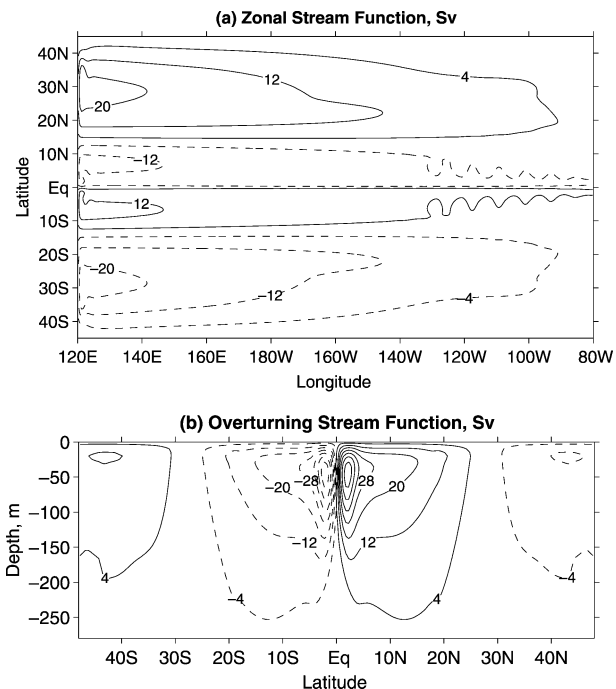


FIG. 16. (a) The vertically integrated streamfunction (integrated from 0 to 300 m) in the large-basin calculations with zero freshwater forcing ( $B = 0$ ). Note the subtropical gyres and western boundary currents. (b) The zonally integrated streamfunction in the large-basin calculations with zero freshwater forcing. Note the strong overturning circulation connecting the Tropics and extratropics (cf. Fig. 4b).

to perennial El Niño conditions can occur rapidly, given freshwater forcing of sufficiently large amplitude.

The consequences of a freshening of the surface waters in high latitudes depend critically on whether the thermohaline or wind-driven circulation is affected most. In the one case the associated climate changes are prominent in low latitudes where there is a tendency towards permanent El Niño conditions. In the other case the climate changes are prominent in high latitudes. What are the factors that determine which of these two components of the oceanic circulation is affected most by a freshening? One likely factor is the degree to which a component contributes to the poleward heat transport. In the Pacific Ocean the wind-driven circulation is the main contributor to the heat transport so that a freshening of the surface waters in the high latitudes of that ocean should have a strong effect on conditions in low latitudes. The Atlantic is a far more complicated matter because there the thermohaline circulation too transports a large amount of heat northward. What are the factors that determine whether a freshening of the waters of the northern Atlantic results in a colder climate for northwestern Europe (in accord with results from studies of the thermohaline circulation) or a deeper equatorial thermocline (in accord with the results presented in this paper)? This is but one of many questions that, at this time, are unanswered.

Further calculations are needed to explore the links

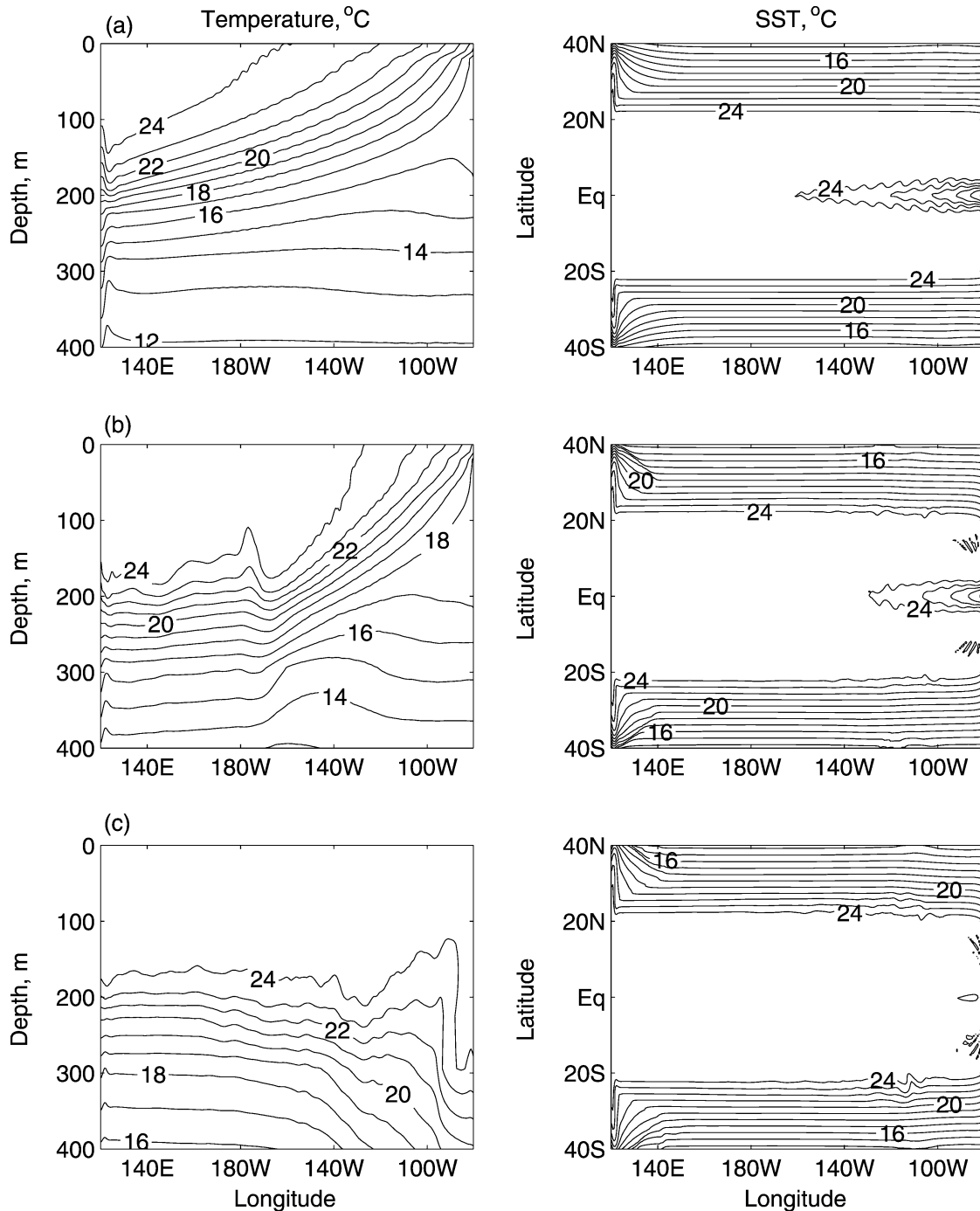


FIG. 17. (left) The thermal structure of numerical solutions in the equatorial plane and (right) the corresponding sea surface temperatures for the large-basin calculations. Notice the collapse of the thermocline in the bottom panels. The freshwater forcing increases from top to bottom [ $B = 0, 0.7, 0.9 (\times 10^{-7} \text{ m s}^{-1})$ ].

between the wind-driven circulation of the Tropics and midlatitudes and the Antarctic Circumpolar Current (Toggweiler and Samuels 1998; Gnanadesikan 1999). Other unanswered questions concern the effect of a collapse of the equatorial thermocline on ocean-atmosphere interactions (e.g., Fedorov and Philander 2000,

2001). Tentative clues are available from the calculations of Dijkstra and Neelin (1995) who find that a deepening of the thermocline can lead to weaker equatorial surface temperature gradients and weaker zonal winds. Such a response could accelerate the tendency toward permanently warm (El Niño-like) conditions. It



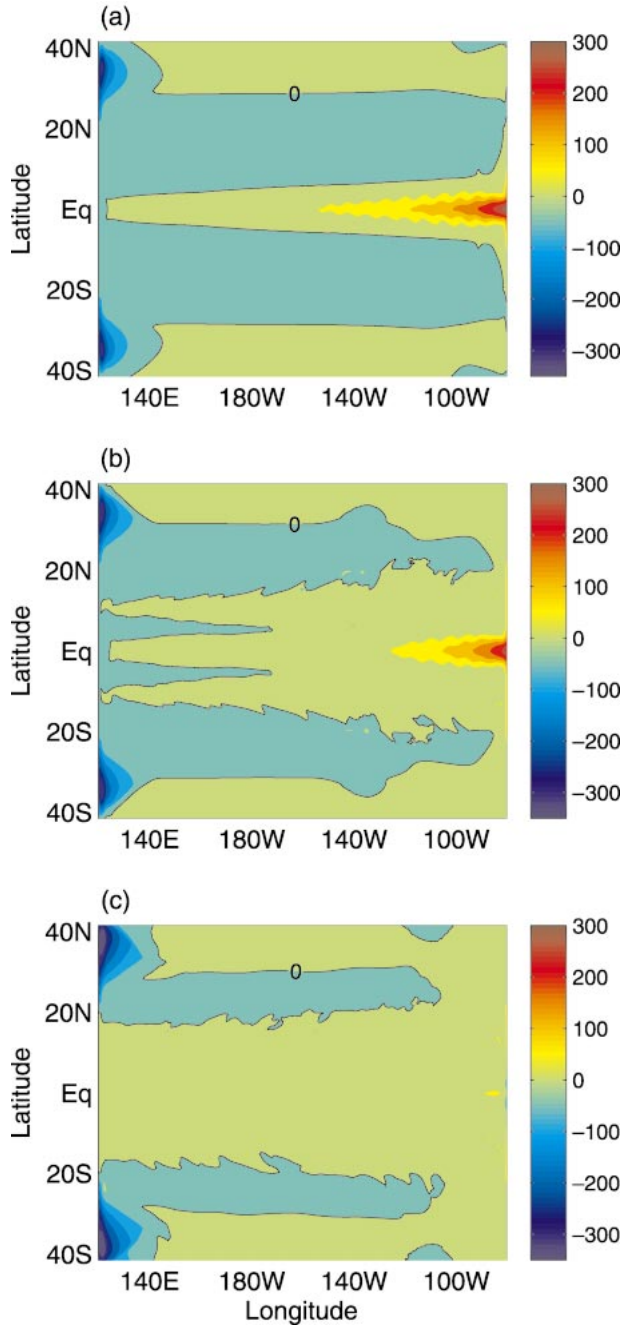


FIG. 18. (a)–(c) The downward heat flux ( $\text{W m}^{-2}$ ) for the solutions shown in the previous figure. The net heat flux into the ocean is zero in (a)–(c). A small positive constant corresponding to a gradual diffusion of heat into the deep ocean was subtracted from the data. Note the qualitative similarities of the simulated heat flux [(a) and (b)] with the observed heat flux (Fig. 1b). In (a) and (b) the heat loss in the extratropics is balanced mainly by the heat gain in the equatorial cold tongue, while in (c) a broad tropical area is needed to balance the heat loss. A significant contribution of the zonal flow to the heat transport accounts for some of the differences between this figure and Fig. 10.

amounts to a positive feedback for the thermocline collapse, but there could also be negative feedbacks and important atmospheric teleconnections that remain to be explored. The investigation of such possibilities is beyond the scope of this paper, which has as its goal merely the exploration of possibilities not previously considered.

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APPENDIX

**Estimation of  $R$  for the Present Pacific Ocean and for the Model**

Estimating the horizontal density ratio  $R$  for the realistic Pacific Ocean is a rather complicated task. The major difficulties arise from four major factors: nonlinearity of the equation of state for saline water, a complex geometry of the ocean, nonmonotonic changes in salinity with latitude, and obvious difference in the ocean density structure between the Southern and Northern Hemispheres. Nevertheless, a very rough estimate can still be made using Figs. 2 and 14. It is convenient to rewrite the definition for  $R$  [Eq. (2)] as

$$R = (\beta/\alpha) * \Delta S / \Delta T, \tag{A1}$$

$\Delta T$  and  $\Delta S$  being the meridional salinity and temperature gradients calculated from the equatorial region to the northern and the southern edges of the subduction zones, off the coast of California and Chili, respectively. (The absolute values for  $\Delta T$  and  $\Delta S$  are used, although their actual values have opposite signs.)

From Fig. 14  $\Delta T \sim 16^\circ\text{C}$ , while  $\Delta S \sim 2$  psu. The ratio  $\beta/\alpha$  varies with temperature from  $3^\circ\text{C (psu)}^{-1}$  in the Tropics to  $5^\circ\text{C (psu)}^{-1}$  in the North Pacific. Taking  $\beta/\alpha = 4^\circ\text{C (psu)}^{-1}$  and the estimates for  $\Delta T$  and  $\Delta S$  gives  $R = 4 \times 2/16 = 0.5$ . Although it is difficult to put error bars on this number, it is still possible to estimate the upper and lower limits on it since the main uncertainty is due to  $\Delta S$ . Reducing  $\Delta S$  to 1.5 gives  $R = 0.4$ , while increasing  $\Delta S$  to 2.5 gives  $R = 0.6$ . Further taking into account the uncertainties in  $\beta/\alpha$ , we could claim that the actual value of  $R$  should lie between 0.3 to 0.7.

In the small-basin calculations the subduction of cold water occurs near the southern and northern walls; a fully nonlinear equation of state for saline water is used. To that end, in order to estimate  $R$  for each numerical run, we simply measure  $\Delta T$  and  $\Delta S$  from the equator to the walls along the middle meridian of the basin. Then  $R$  is calculated using relation (A1) and the same ratio  $\beta/\alpha = 4^\circ\text{C (psu)}^{-1}$ .

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